

Femto-UP 2020-21 School

# Femtosecond Pulse Generation

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# Definitions





# Many properties





# Time-resolved spectroscopy



Electric field of a 10-fs 800-nm pulse



Time-resolved spectroscopy Direct observation of ultrafast motions



Δ



→ time



Ahmed Zewail, Nobel Prize in chemistry 1999, femtochemistry

# Imaging



Electric field of a 10-fs 800-nm pulse



High peak power (Energy /Duration)

Nonlinear microscopy



# Material processing



Electric field of a 10-fs 800-nm pulse



High peak power (Energy /Duration)

Laser matter interaction

Drilling, cutting, etching,...





B. Chichkov et al, Appl. Phys. A. 63, 109 (1996)

Areas of applications : aeronautics, electronics, medical, optics...

# Light matter interaction



#### Electric field of a 10-fs 800-nm pulse



#### High peak power (Energy /Duration)

# Ability to reach extreme conditions (amplified system)

Applications : Sources of intense particles beams, X-rays, high energy density science, laboratory astroprophysics ...



# Metrology



#### Electric field of a 10-fs 800-nm pulse



**Spectral Properties** (Frequency Comb)









J.L. Hall T.W. Hänsch

Nobel Prize 2005 "for their contributions to the development of laser-based precision spectroscopy, including the optical frequency comb technique." 8



Introduction

- 1. Description of ultrashort light pulses
- 2. Generation of femtosecond laser pulses via mode locking
- 3. Femtosecond oscillator technology

# Introduction





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#### Ultrashort pulse = broad spectrum



What makes the difference between white light and femtosecond pulses ?

### **Definitions : Electric fields**



#### E(t) Real electric field



### Ultrashort pulse = sum of monochromatic waves

$$E(t) = \int_{-\infty}^{\infty} E(\omega) \exp(-i\omega t) \frac{d\omega}{2\pi} = TF[E(\omega)]$$

$$E(\omega) = \int_{-\infty}^{\infty} E(t) \exp(i\omega t) dt = TF^{-1} [E(t)]$$

# **Definitions : Complex electric fields**





# **Definitions : Complex electric fields**





# **Definitions : Intensity**







Gaussian envelope centered on the carrier frequency





#### **Temporal intensity**

 $I(t)=\exp(-rac{t^2}{a^2})$ 

RMS width

 $\Delta t = a/\sqrt{2}$ 

#### Spectral intensity

$$I(\omega) = \exp(-a^2(\omega-\omega_0)^2) \qquad \qquad \Delta \omega = 1/a\sqrt{2}.$$



0.9



#### **Temporal intensity**

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Spectral intensity

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RMS width
$$\Delta t = a/\sqrt{2}$$

$$\Delta t \Delta \omega = 1/2$$

$$\Delta t$$

0.9



#### **Temporal intensity**

 $I(t)=\exp(-rac{t^2}{a^2})$ 

Spectral intensity

$$I(\omega)=\exp(-a^2(\omega-\omega_0)^2)$$

RMS width
$$\Delta t \Delta \omega = 1/2$$
 $\Delta t = a/\sqrt{2}$ The uncertainty limit is only  
reached for Gaussian pulses $\Delta t \Delta \omega = 1/2$ Image: Comparison of the two stress of t



#### **Temporal intensity**

 $I(t)=\exp(-rac{t^2}{a^2})$ 

**FWHM** Full Width at Half Maximum

$$\Delta t_{1/2} = \sqrt{8ln2}\Delta t = 2.355\Delta t$$

$$\Delta t_{1/2}\Delta \omega_{1/2}=4ln2$$

Spectral intensity

$$I(\omega)=\exp(-a^2(\omega-\omega_0)^2)$$

For  $\lambda = 1 \mu m$  Pulse duration = 100 fs / Spectral bandwidth = 14,6 nm





### Temporal profile and spectral phase





$$\varepsilon(\omega) = |\varepsilon(\omega)| \exp(i\varphi(\omega))$$

### Temporal profile and spectral phase







$$egin{split} \mathscr{E}(\omega) &= |\mathscr{E}(\omega)| \exp(i arphi(\omega)) \ arphi(\omega) &= arphi(\omega_0) + arphi'(\omega_0)(\omega-\omega_0) + rac{1}{2} \, arphi''(\omega_0)(\omega-\omega_0)^2 + rac{1}{6} \, arphi'''(\omega_0)(\omega-\omega_0)^3 + \dots \end{split}$$

 $\tau_g(\omega) = \varphi'(\omega)$  Group delay = relative delay of a spectral component

### Effects of the spectral Phase





### Effects of the spectral Phase







$$\mathscr{E}(\omega) = |\mathscr{E}(\omega)| \exp(i\varphi(\omega))$$

$$\varphi(\omega) = \varphi(\omega_0) + \varphi'(\omega_0)(\omega - \omega_0) + \frac{1}{2}\varphi''(\omega_0)(\omega - \omega_0)^2 + \frac{1}{6}\varphi'''(\omega_0)(\omega - \omega_0)^3 + \dots$$

$$\tau_g(\omega) = \varphi''(\omega_0)(\omega - \omega_0)$$
The group delay varies linearly with the frequency
$$t$$

# Parabolic spectral phase





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Spectral phase accumulated by propagation :

 $arphi(z,\omega)=arphi(0,\omega)+k(\omega)z \qquad \qquad k(\omega)=n(\omega)\omega/c$ 

$$au_g(z,\omega)= au_g(0,\omega)+k'(\omega_0)z+(\omega-\omega_0)k''(\omega_0)z+\dots$$



Spectral phase accumulated by propagation :

 $arphi(z,\omega)=arphi(0,\omega)+k(\omega)z \qquad \qquad k(\omega)=n(\omega)\omega/c$ 

$$\tau_g(z,\omega) = \tau_g(0,\omega) + k'(\omega_0)z + (\omega - \omega_0)k''(\omega_0)z + \dots$$
Constant delay
$$V_g(\omega) = 1/k'(\omega)$$
Group velocity
(velocity of the envelope)



Spectral phase accumulated by propagation :

 $arphi(z,\omega)=arphi(0,\omega)+k(\omega)z \qquad \qquad k(\omega)=n(\omega)\omega/c$ 





What is the output pulse after propagation in a material with k">0?



### Quizz





### Duration after propagation in a dispersive material



Materials transparent in the visible : k">0



Dispersive effects higher for shorter pulses

 $au_g(z,\omega)= au_g(0,\omega)+k'(\omega_0)z+(\omega-\omega_0)k''(\omega_0)z+\dots$ 

# Summary 1



- $\varepsilon(\omega) = |\varepsilon(\omega)| \exp(i\varphi(\omega))$
- ✓ Short Pulse = broad spectrum

$$\Delta t \Delta \omega \ge \frac{1}{2}$$

- $\checkmark$  The spectral phase governs the temporal shape
- ✓ Non linear spectral phase = group velocity dispersion
- Propagation in transparent material = up chirped pulse



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# Fundamental of mode locking





# Gain medium




#### $\mathbb{A} = \mathbb{A} =$ $\phi_n(t)$ $\omega_n$ Example : $\phi_{n+1}(t)$ $^{\Lambda}$ $\omega_{n+1}$ $\lambda = 800 nm$ $\phi_{n+2}(t)$ $\omega_{n+2}$ $\Delta \lambda = 80 nm$ $\phi_{n+3}(t)$ $\omega_{n+3}$ N modes >100 000 $\omega_{n+4} = \phi_{n+4}(t)$ ... how when the mark of the second the second second Random phase modes $I(t) = I_0 igg[ rac{\sin(N\delta\omega t/2)}{\sin(\delta\omega t/2)} igg]^2$ In-phase modes : $\phi_n(t) = 0$ $2\pi/\delta\omega$ $\delta\omega = 2\pi \frac{c}{2L}$ 37

## Longitudinal modes

#### in time domain

### Mode locking





Mode locking = phases locked $\phi_n = n\alpha$ Train pulses separated by the round trip timeSpectral width increases with NDuration decreases with N

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### Mode locking





Idea :to favor pulsed regime over continous one

Loss modulation

- Active modelocking
   Acousto-optic modulator
  - ➢Electro-optic modulator
- Passive modelocking
  KLM
  SESAM

Figure from book chapter Ultrafast solid-state lasers, Ursula Keller



### Active modelocking





# Acousto-optic (or electro-optic) modulator synchronized with the resonator round trip



Generation of a grating that turns ON and OFF at a frequency  $2\Omega = c/2L$ 



Self amplitude modulation of the light by **fast** loss saturation

Shorter pulse Starting with noise fluctuations



- Kerr Lens
- Saturable absorber



Kerr effect: Nonlinear change in refractive index  $n(r) = n_0 + n_2 I(r)$ Fast (few fs) and broadband



KLM = Kerr Lens Modelocking

Self focusing + hard or « soft » aperture

Not self starting : vibrating mirror or saturable absorber

### Saturable absorber

Saturable absorber : component with losses reduced by high intensities







How to compensate for the dispersion in the cavity?



DVG >0 in the visible

- ✓ Prisms
- ✓ Gratings
- ✓ Chirped mirrors

Dispersion management with prisms



Prism sequence for adjustable group delay dispersion.

angular dispersion



Dispersion management with prisms



Prism sequence for adjustable group delay dispersion.



### Dispersion management with prisms





### Dispersion management with gratings



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p diffraction order
d grating pitch
I angle of incidence
θ angle of the reflected wavelength

$$\frac{d^2\varphi}{d\omega^2} = \frac{-8\pi^2 cL}{\omega^3 d^2 \cos^3 \theta} < 0 \qquad (p=1)$$

$$\frac{d^3\varphi}{d\omega^3} = \frac{12\pi^2 cL}{\omega^4 d^2} \frac{1 + \frac{2\pi c}{\omega d} \sin i - \sin^2 i}{\cos^5 \theta} > 0$$

### Dispersion management with gratings





- ✓ negative group delay
   ✓ Distance between gratings
   ✓ Gratings pitch
- $\checkmark$  4 gratings or 2 gratings in double pass

✓ much more dispersive than prisms but introduces higher losses

### Dispersion management with chirped mirror



Bragg mirror with variable layer thickness values



#### ✓Compact

✓ High reflectivity

✓ Can compensate for higher orders

✓ Fixed GDD -> multiple
 reflections





The repetition rate of a femtosecond oscillator is related to:

- The acousto-optic modulator
- The length of the cavity
- the pulse width

1 2 3



The repetition rate of a femtosecond oscillator is related to:

• The length of the cavity





### Summary 2





 $\Delta \omega = 2\pi rac{c}{2L}$  53

### Frequency comb





Discrete and perfectly equally spaced frequency lines

➢ frequency etalon

### The carrier enveloppe phase





- $f_r$  Repetition rate 100MHz-GHz
- $f_0$  Carrier Enveloppe Offset (CEO)

For very short pulse, difference between phase and group velocities matters

$$f_0 = \frac{\Delta \phi_{CE}}{2\pi} f_r$$
$$\Delta \phi_{CE} = L\omega_0 \left(\frac{1}{v_g} - \frac{1}{v_\varphi}\right)$$

### Frequency comb for optical clock





https://www.nist.gov/programs-projects/femtosecond-laserfrequency-combs-optical-clocks  $f_r$  and  $f_0$  are **Microwave frequencies** (100MHz-GHz) linked to **optical frequencies** (THz)





### A revolution in the measure of time/frequency





### Frequency comb evolutionary tree



#### fs oscillator = « comb generator »





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### Femtosecond oscillator technology



✓ Ti:Sapphire oscillators

✓ Yb:bulk oscillators

✓ Fiber-based oscillators





### Laser specifications



Energy	Energy per pulse	Joule
Average power	Energy per unit time	Watt
Peak power	Maximum power	Watt
Intensity (irradiance)	Peak power per unit area	Watt/cm2



### Quizz



### Quizz



Pulse width10 fsEnergy10 nJRepetition rate100 MHzAverage power?1 W = 10 nJ x 100 MHzPeak power?1 MW = 10 nJ / 10fsEnergy



### **Ti:Sapphire oscillator**



#### Sapphire crystals doped with ions Ti3+





Good thermal conductivity

Very broad gain bandwidth from 650 nm to 1100 nm Large emission cross section (41. 10<sup>-20</sup> m2 @ 780 nm)



Extreme tunability and short duration

### **Ti:Sapphire oscillator**

Large quantum defect (energy difference between pump and laser photons)

Pump : green CW laser (DPSS : frequency doubled diode-pumped laser)

YVO4



SHG





diodes

Energetically inefficient, complex and expensive



### Ti :Sapphire cavity

LippB Laboratoire d'Optique et Biosciences



### Pulses in the two-cycle regime





Interferometric autocorrelation



Pulse duration ~5fs

D. H. Sutter, G. Steinmeyer, L. Gallmann, N. Matuschek, F. Morier-Genoud, U. Keller, V. Scheuer, G. Angelow, and T. Tschudi, "Semiconductor saturable-absorber mirror–assisted Kerr-lens mode-locked Ti:sapphire laser producing pulses in the **two-cycle regime**," Opt. Lett. **24**, 631-633 (1999)

### Ti:Sapphire commercial lasers





0,7 W, 700-1080 nm, <100fs



2,5 W, 690nm- 1020 nm, 140fs

Repetition rate : 80MHz



#### Ti:Sa today :

 Expensive and not very effective but reliable, tunable, and very short pulsewidth
 Many applications : bio-imaging, ultrafast spectroscopy, high field physics, amplifier seeding,...

### **Ytterbium : bulk oscillator**





Many different hosts for Ytterbium ions : YAG, glass, KYW, CaF2, ... Low quantum defect : high power efficiency, reduced thermal effects Great advantage : **diode pumping** at 980 nm

### **Ytterbium : bulk oscillator**





Pulse width : 300 fs Repetition rate : 50 MHz Energy : a few 100s nJ **High average power**  ✓ SESAM

✓ Prisms or chirped mirrors

### Ytterbium : bulk oscillator





Average Power	> 1,3 W
Energy Per Pulse	>24 nJ
Pulsewidth	< 250 fs
Repetition Rate	54 MHz
Central Wavelength	1025 +/- 5 nm



Average Power	>1.5 W
Wavelength	1045 ±8.0 nm
Repetition Rate	63 MHz
Pulse Width (FWHM)	<250 fs
Pulse Energy	>24 nJ
Peak Power	>80 kW

- ✓ High average power
- ✓ Low cost per watt
- ✓ Compact
- ✓ Pulse duration 300fs

### **Fiber-based oscillators**



### Gain media : fiber doped with Rare Earth ions (Large gain bandwidth)


## Fiber-based oscillators



### **Conventional laser**





#### Fibre laser





Large surface area Guided mode Heat resistance of silica



# Simple cavity of fiber-based oscillators





### Fiber-based oscillators

✓ Long propagation distance : High gain, low thermal effects

- ✓ Spatial quality
- ✓ Stability
- ✓ Compactness
- ✓Cost effective

Large variety of designs and specifications

1 W , 200fs , 1045 nm , 50 MHz fs pulses delivered by optical cable











✓ Ultrashort pulses = broad spectra -> Large dispersion effects

✓ Description in both time and frequency domain

✓ Generation via modelocking thanks to nonlinear effects

✓ Wide variety of femtosecond lasers