

Coherent multidimensional spectroscopies: advanced spectroscopic techniques to unveil complex dynamics

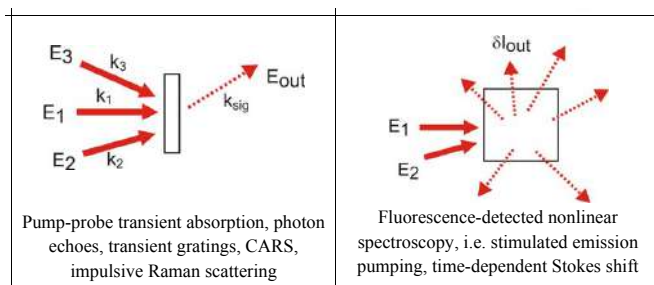
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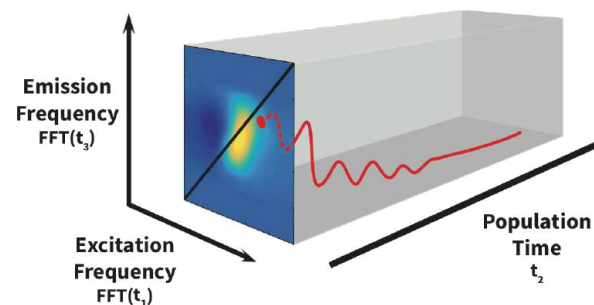
Femto-UP 2020-21: Ultrafast lasers technologies and applications

8-29 Mar 2021 Online (France)

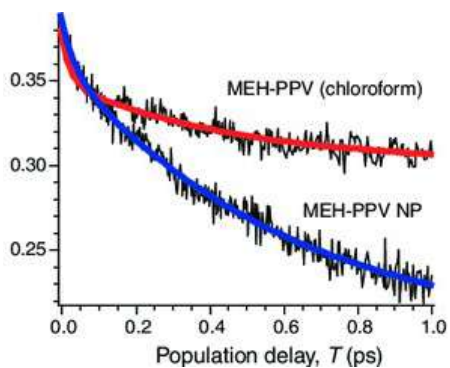
'coherent'



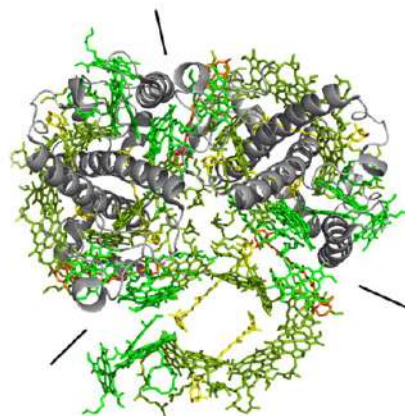
'multidimensional'



'dynamics'



'complex'





A second dimension was introduced for the first time in NMR spectroscopy,
NOESY (nuclear Overhauser enhancement spectroscopy)
COSY (correlation spectroscopy)
These techniques have been extensively used to study structural and dynamical properties of proteins in solution.

In the optical regime, the origin of multidimensional vibrational spectroscopy can be traced to the coherent anti-Stokes Raman spectroscopy (CARS) measurements of vibrational dephasing performed in the 1970s.

2D vibrational spectroscopic technique (2D-IR) can provide detailed information on the 3D structure of a given complex molecule, i.e., proteins, water networks,...

2D electronic spectroscopy was introduced by Fleming
Delay with respect to the IR counterpart due to experimental problems connected with the higher frequency of Visible light.

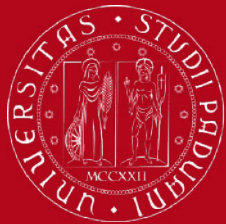
**2D-
NMR
1970**



**2D-IR
1980-90**



**2D-ES
2000**



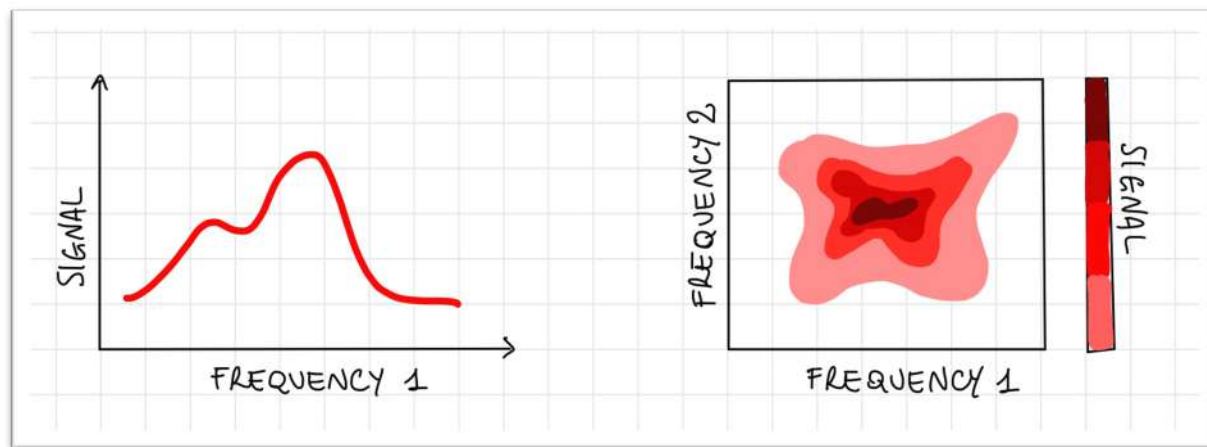
CMDS techniques can be declined at different orders of the nonlinear polarizability (3° , 5° , etc.) and in different spectral ranges (IR, Vis, UV...)

2D electronic spectroscopy:

- third order technique: generalized version of a 4-wave mixing spectroscopy
- in the Vis range: electronic transitions

2D electronic spectroscopy (2DES): why and when?

Conventional optical spectroscopy techniques, such as ordinary infrared, Raman, and UV-visible spectroscopies, provide a one dimensional (1D) projection of the available molecular information of a sample onto a single frequency axis. In contrast, optical multidimensional (2D, 3D) spectroscopy techniques provide a multidimensional projection of the relevant molecular motions offering dramatically more information.



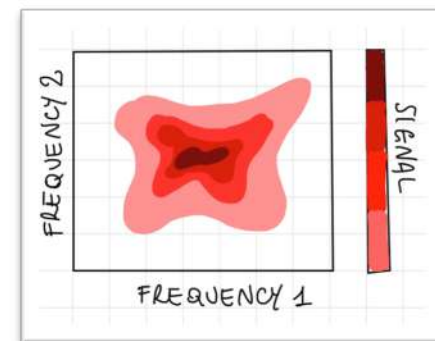
why 2DES ?

NUMBER OF OBSERVABLES
(PEAKS)
 $\sim N$ (1D)
 $\sim N^2$ (2D)
 $\sim N^d$ (d-dimensional spectroscopy)

- Spread information along multiple dimensions
- Simultaneously frequency and time-resolved
- Couplings and transport processes mapped far from diagonal positions (where main dynamical processes take place)
- Sensitivity to coherent dynamic mechanisms (oscillations)

Why not?

- complex (and expensive) optical setups
- demanding data processing and analysis
- challenging interpretation of the data (artefacts)



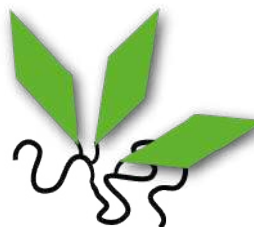
ideal to untangle complex dynamics (transport processes)
in complex multichromophore systems

biological antennas

JPCLet11(2020)1059
NatureComm9(2018)3160



JPCLet7(2016)4996
**strongly coupled
J-aggregates**



JPCLet11(2020)7972

**porphyrin-peptide
self assemblies**



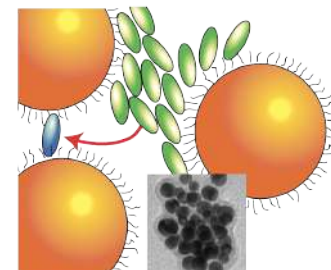
PCCP22(2020)7516

**rhodamine dimers
on DNA**



Nanoscale(2021)
10.1039/D1NR00775K

**hybrid
metal-organic
nanomaterials**

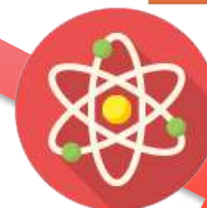
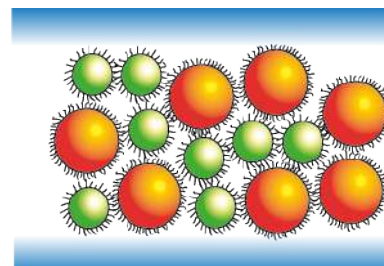


**porphyrin
functionalized
oligomers**

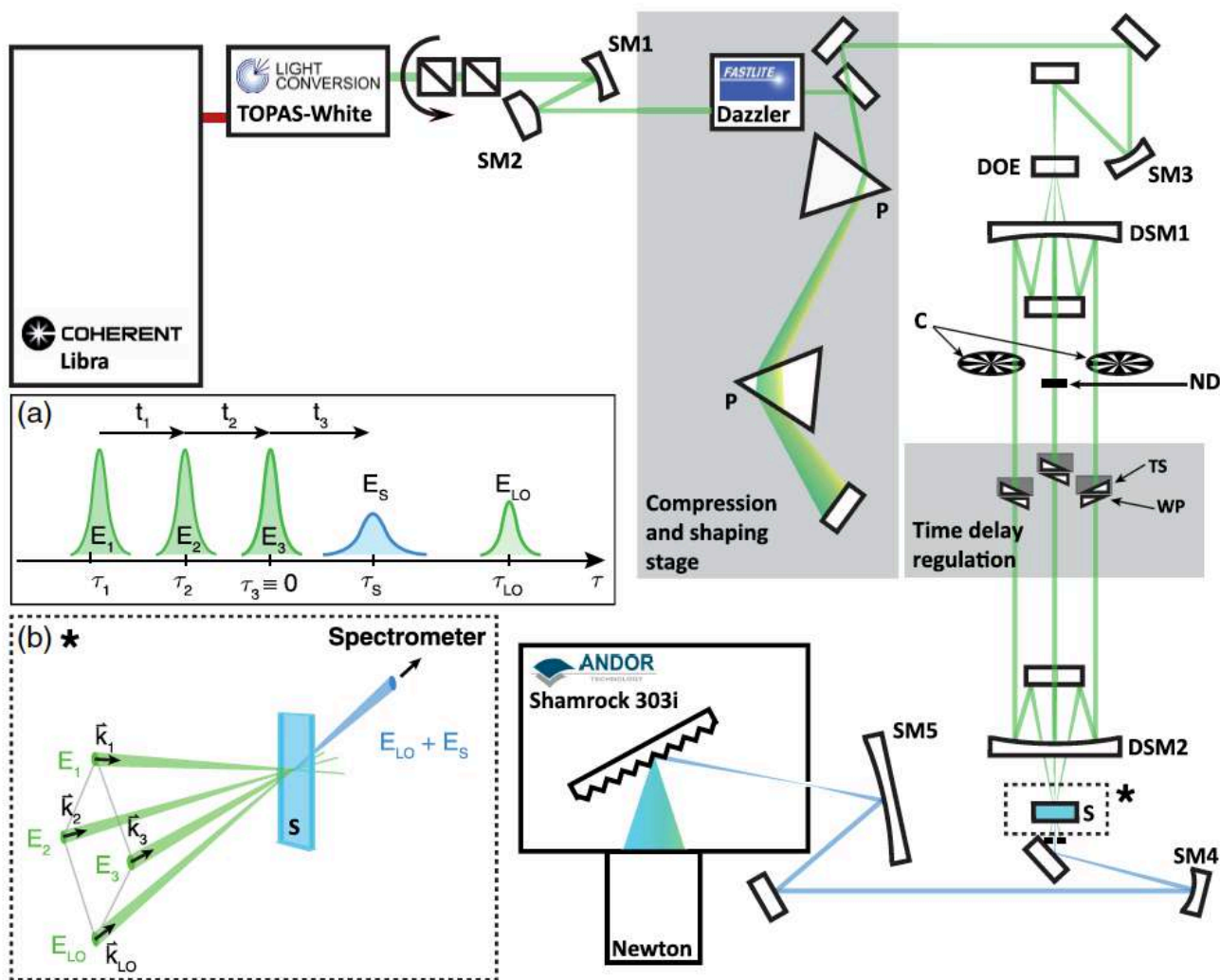
JPCC123(2019)10212

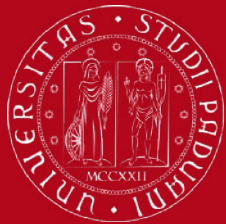
**transport in QDs
materials**

JPCC124(2020)16222
JPCC123(2019)31286
JCP154(2021)014301



2D electronic spectroscopy: the experiment

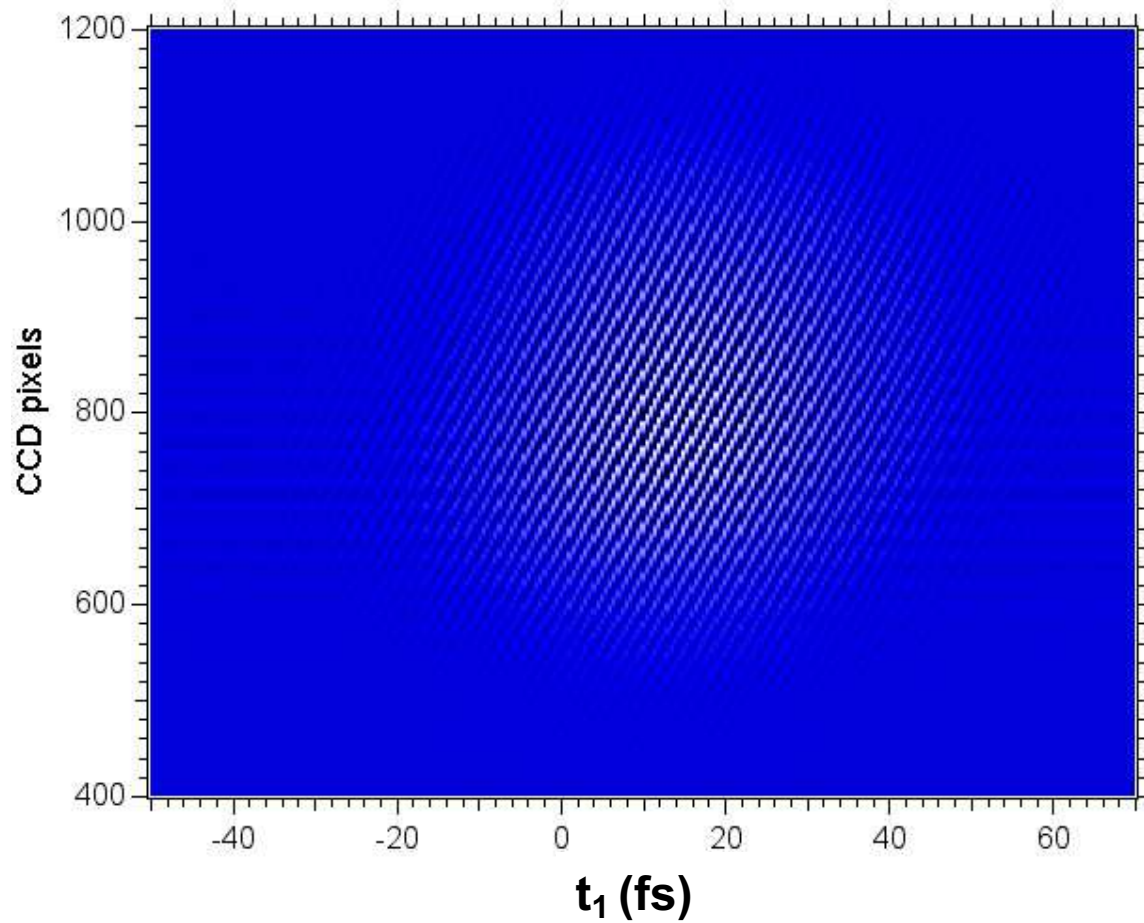
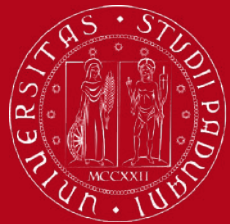




$$I_{\text{det},HOMO} = \frac{nc}{8\pi} |E_S|^2$$
$$I_{\text{det},HET} = \frac{n(\omega_S)c}{4\pi} |E_{LO}(t) + E_S(t)|^2 =$$
$$= I_{LO} + I_S + 2 \frac{n(\omega_S)c}{4\pi} \text{Re}[E_{LO}^*(t) \cdot E_S(t)]$$

The heterodyne signal is linear rather than quadratic in the (weak) signal field

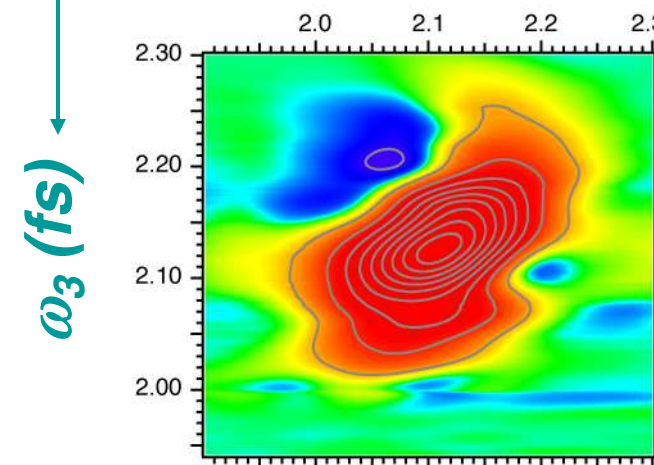
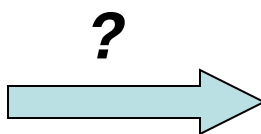
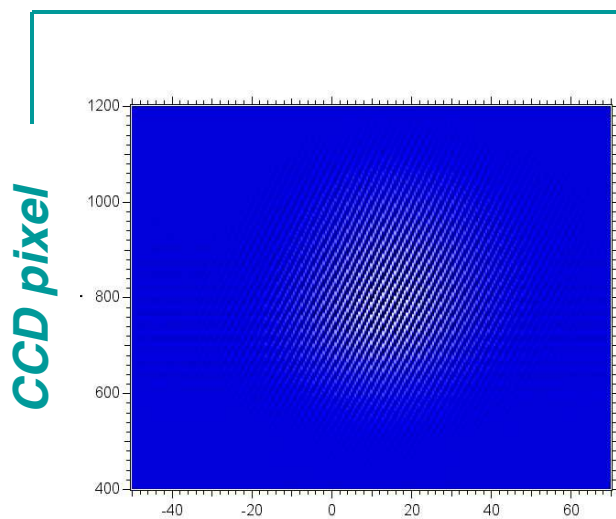
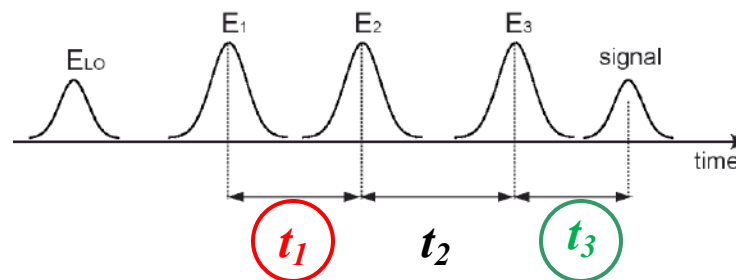
By controlling the relative phase of E_{LO} and E_S it is possible to probe separately the real and imaginary part \Rightarrow *phase sensitive detection*



From interferograms to 2D spectra

$$I(\omega) = 2\text{Re}\left[E_{LO}^*(\omega) \cdot E_S(\omega) \cdot e^{-i\omega\Delta\tau}\right]$$

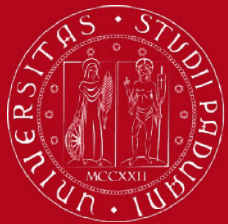
$$E_S(\omega) = \frac{\text{FFT}\left[\theta(t) \text{IFFT}\{I(\omega)\}\right] e^{-i\omega\Delta\tau}}{E_{LO}^*(\omega)}$$



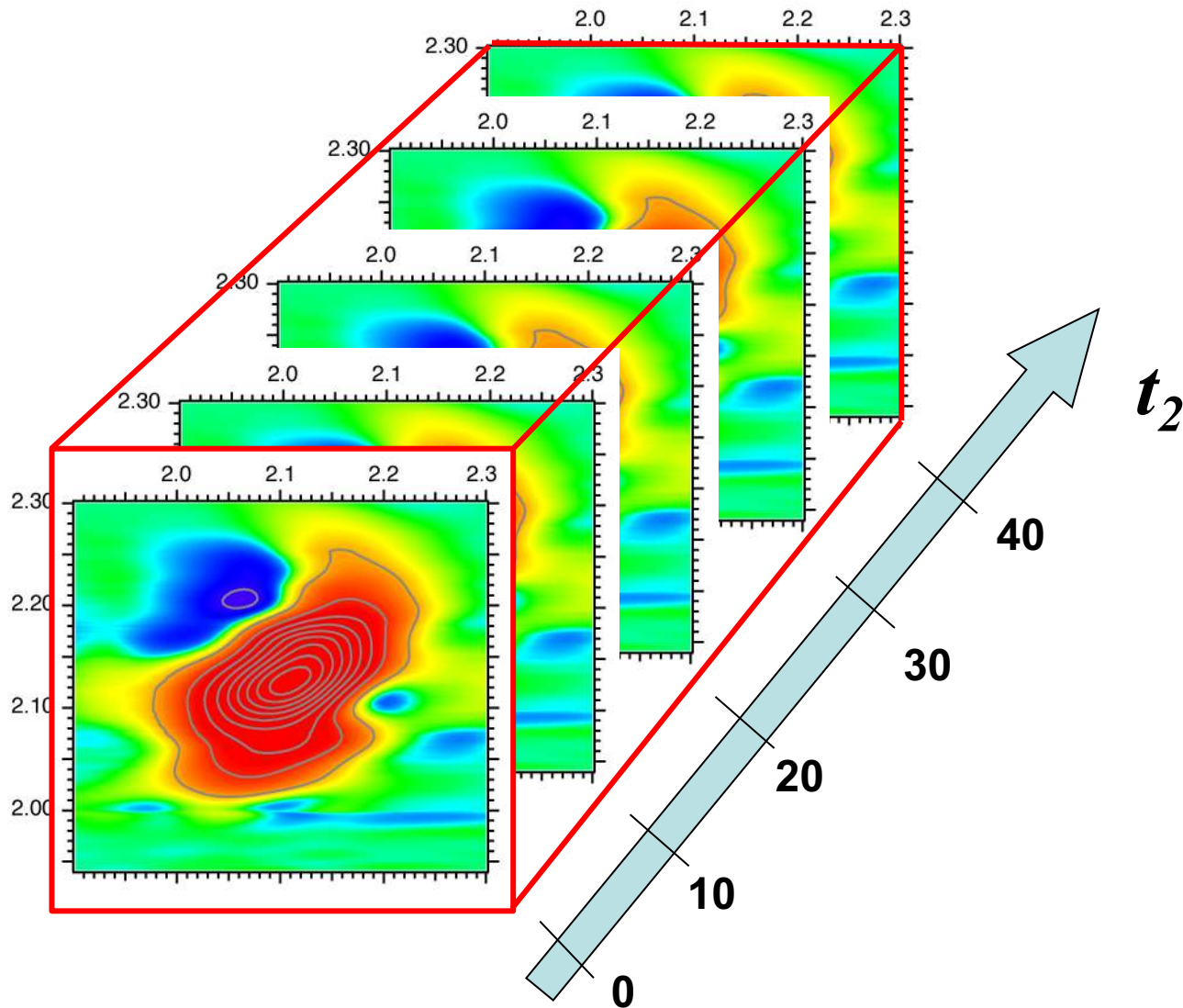
t_1 (fs)

FFT

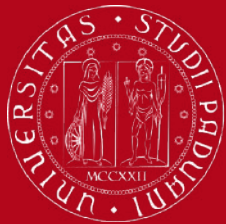
ω_1 (fs)



From interferograms to 2D spectra



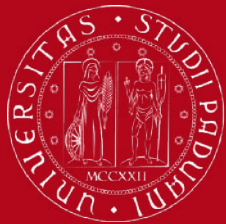
Response Function Formalism



Time-resolved techniques

In the **perturbative approach**, the signal is proportional to the polarization $P(r,t)$, induced in the sample by the interaction with electric fields, expressed as convolution between the fields and with the molecular response function $R^{(n)}$:

$$P_i^{(n)}(t) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \dots \int_{-\infty}^{+\infty} dt_1 dt_2 \dots dt_n R_{ijk\dots l}^{(n)}(t - t_1, t - t_2, \dots, t - t_n) \times \\ E_j(t_1) E_k(t_2) \dots E_l(t_n)$$



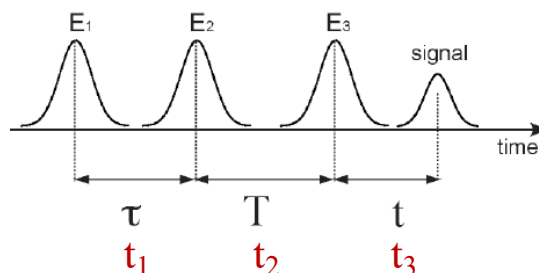
$$P_i^{(n)}(t) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \dots \int_{-\infty}^{+\infty} d\omega_1 d\omega_2 \dots d\omega_n \chi_{ijk\dots l}^{(n)}(\omega_1, \omega_2, \dots, \omega_n) \times \\ E_j(\omega_1) E_k(\omega_2) \dots E_l(\omega_n) \exp[-i(\omega_1 + \omega_2 + \dots + \omega_n)t]$$

$$\chi^{(n)}(\omega_1 \dots \omega_n) = \int_{-\infty}^{+\infty} \dots \int_{-\infty}^{+\infty} dt_1 \dots dt_n R_i^{(n)}(t_1 \dots t_n) \exp\left(-i \sum_{j=1}^n \omega_j t_j\right)$$

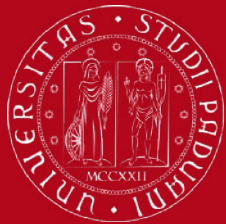
The susceptibility $\chi^{(n)}(\omega_1 \dots \omega_n)$ is the Fourier-Laplace transform of the response function $R_i^{(n)}(t_1 \dots t_n)$

The most general time-resolved experiment related to $P^{(3)}$ requires the interaction with 3 fields and it can be generally indicated as **four wave mixing**. In the impulsive limit (very short pulses) the signal is directly related to the response function $R^{(3)}$.

It is possible to change the relative time ordering and the phase-matching of the 3 interactions: in this way the signal becomes sensitive only to specific processes, and different techniques may be distinguished (pump&probe, photon echo, transient grating, hole burning,...)



$$P_i^{(3)}(t) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} dt_1 dt_2 dt_3 R_{ijk}^{(3)}(t-t_1, t-t_2, t-t_3) \times E_1(t_1) E_2(t_2) E_3(t_3)$$



$$R_{ijk}^{(3)}(t-t_1, t-t_2, t-t_3) = \sum_{\alpha} R_{\alpha}^{(3)}(t-t_1, t-t_2, t-t_3)$$

$R^{(3)}$ can be calculated within the **perturbation theory** framework using **Feynmann diagrams**. Depending on the pulse order and on the phase matching conditions, only selected diagrams (=evolution pathways along the **density matrix**) will be relevant and this simplify the calculation of the signal.

density matrix

$$\rho(t) \equiv |\psi(t)\rangle\langle\psi(t)|.$$

$$\langle A \rangle = \langle \psi | A | \psi \rangle = \text{Tr}[A\rho].$$

———— *b*

$$\begin{bmatrix} \rho_{aa} & \rho_{ab} \\ \rho_{ba} & \rho_{bb} \end{bmatrix}$$

———— *a*

$\begin{bmatrix} \mathbf{1} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix}$ The system is described by ψ_a
(only the *a* state is populated)

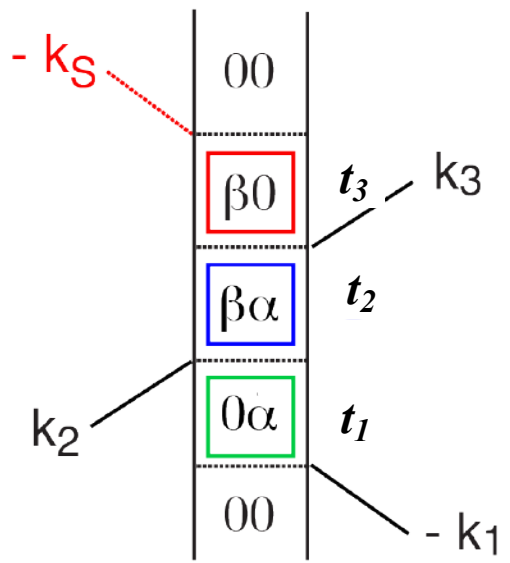
$$\begin{bmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

The system is described by a coherent superposition of *a* and *b* states:

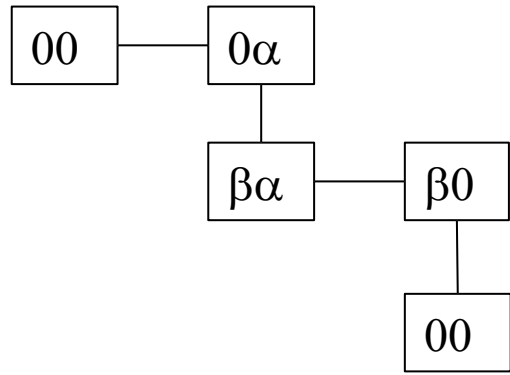
$$\frac{1}{2}\psi_a + \frac{1}{2}\psi_b$$



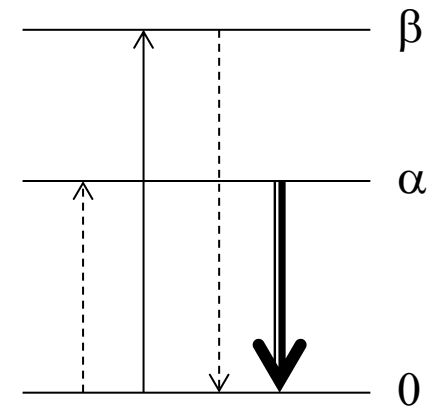
Feynman diagram



Liouville diagram

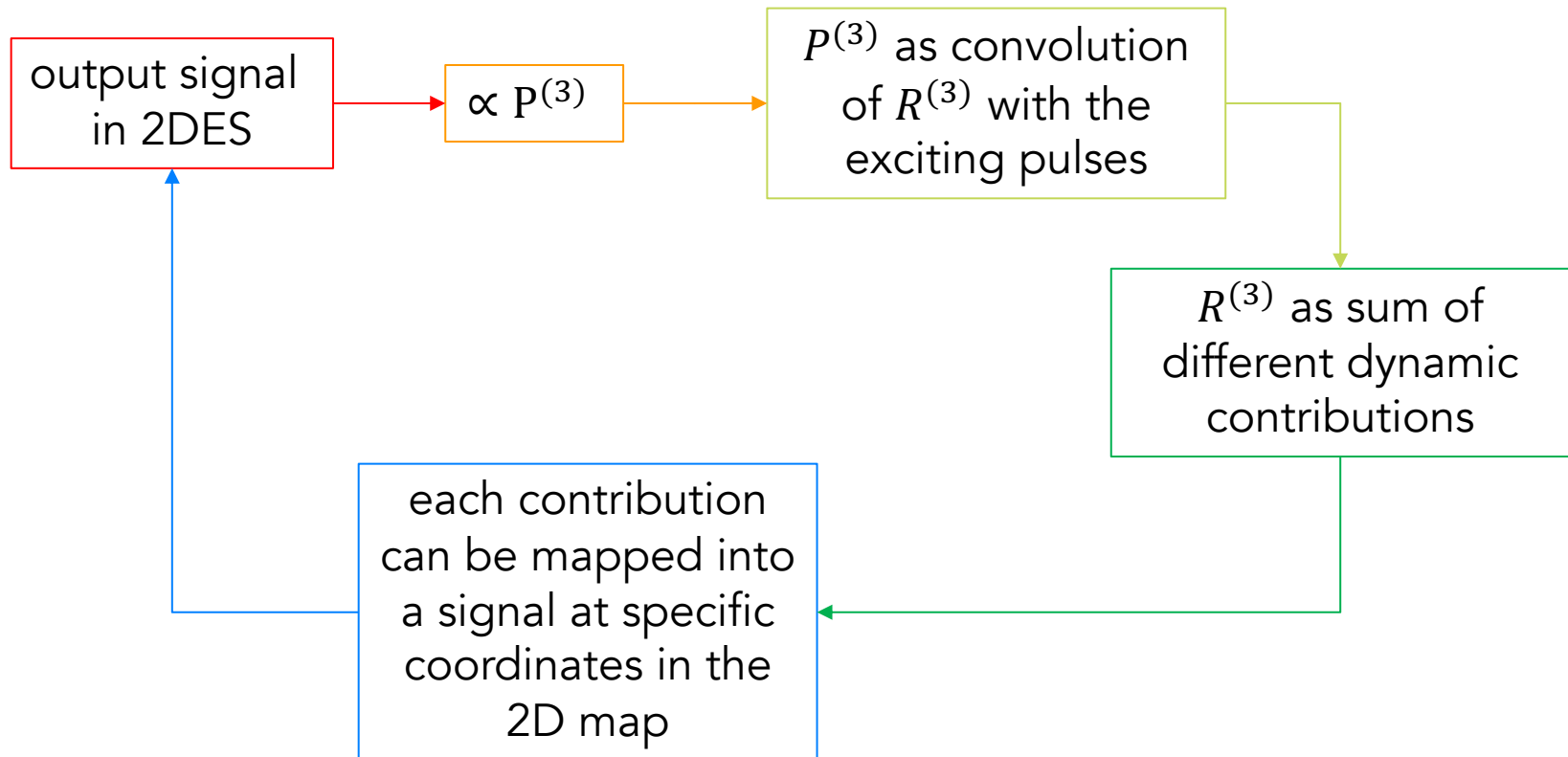


levels diagram



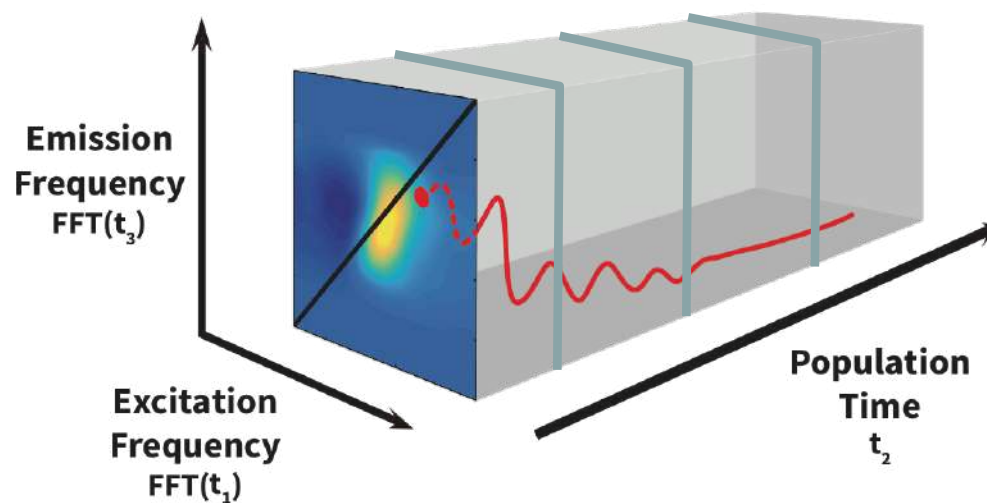


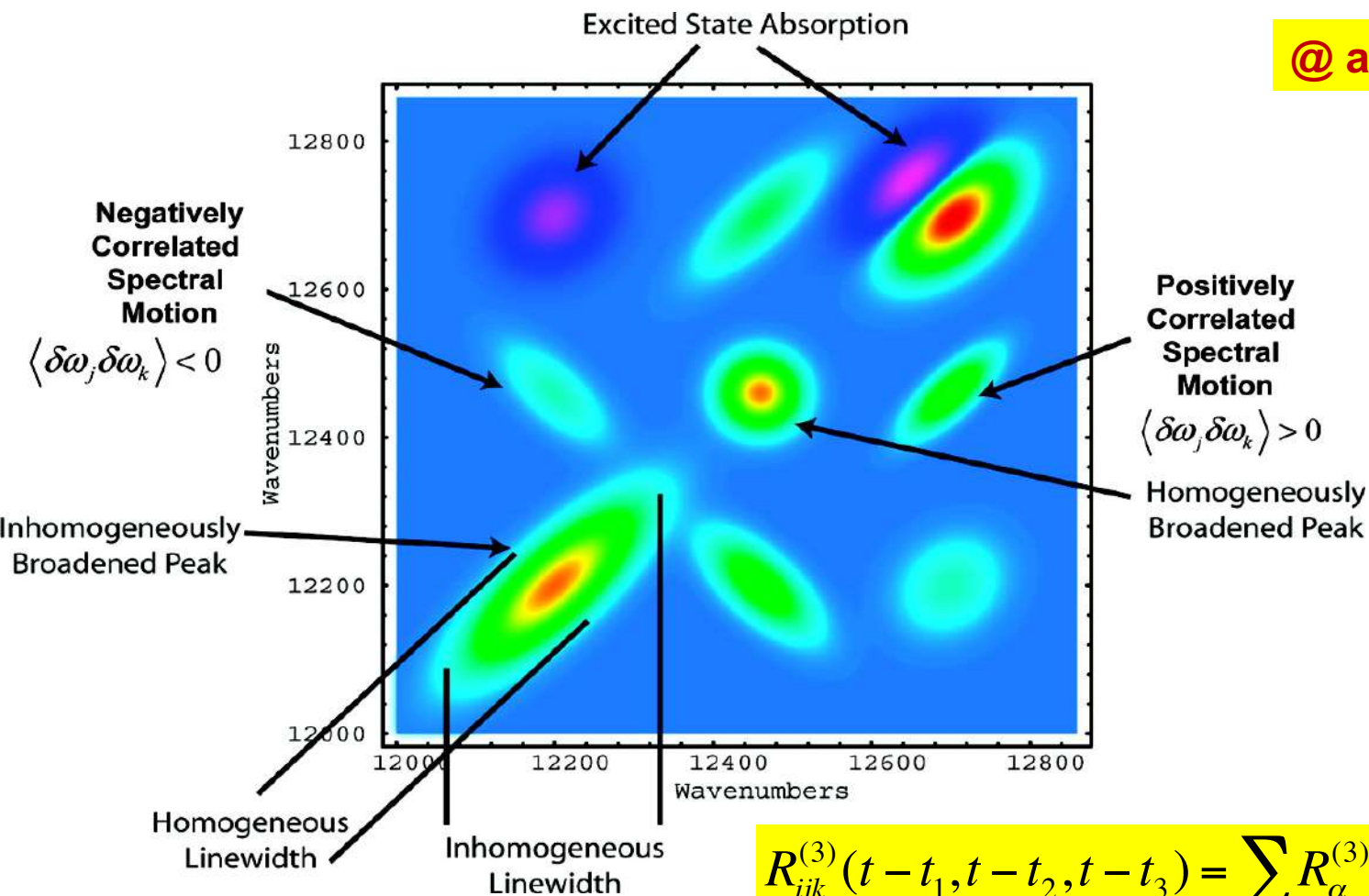
signal, response functions and evolution pathways



2D electronic spectroscopy: qualitative description of the response

2DES: off-diagonal cross-peaks resolve couplings between states

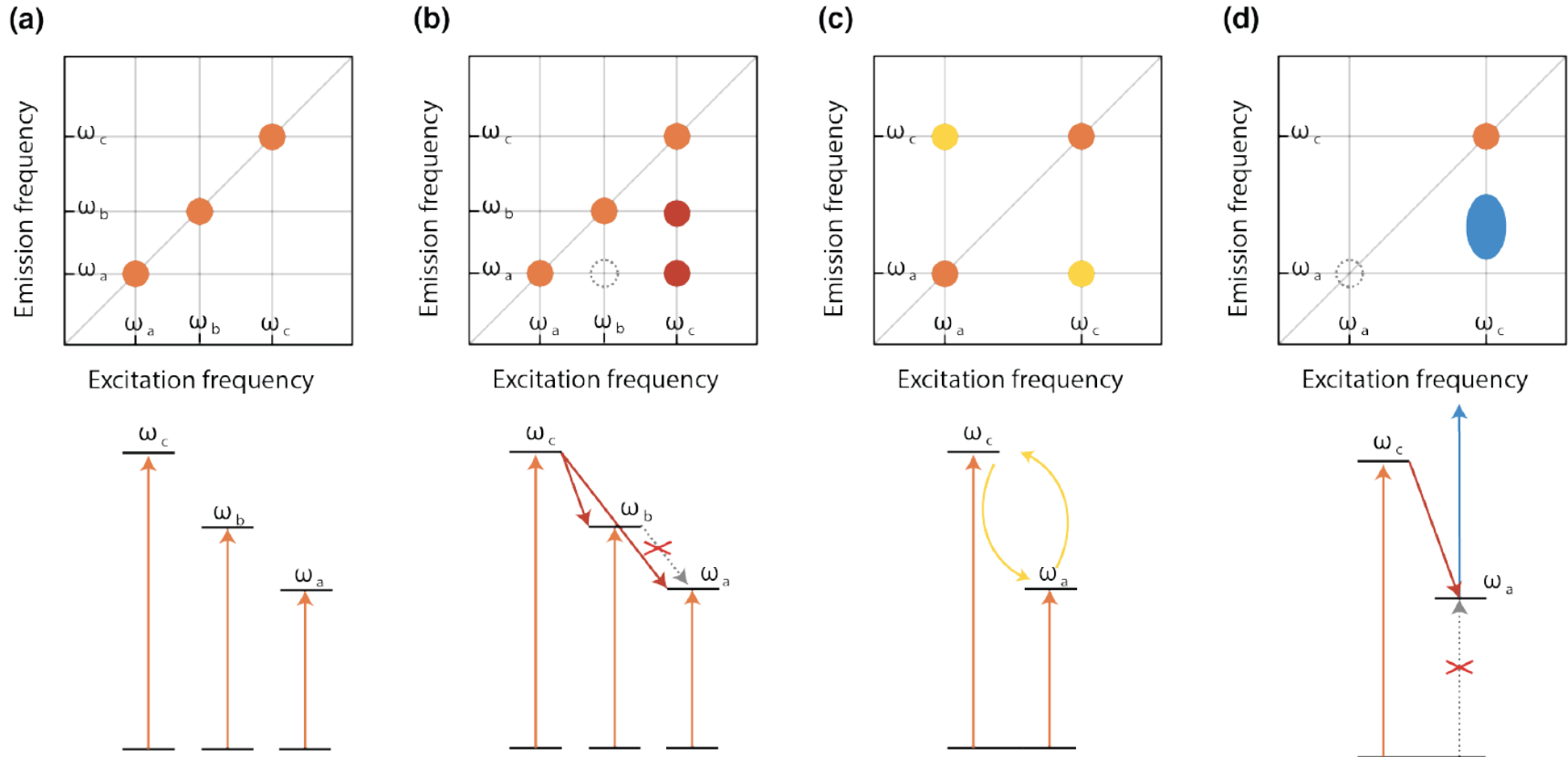




@ a fixed value of t_2

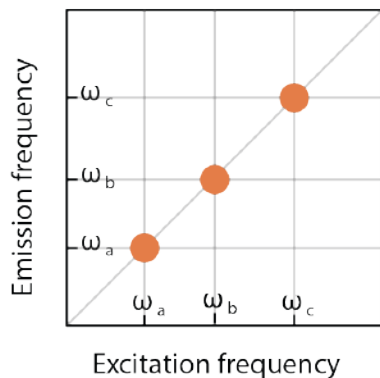
$$R_{ijk}^{(3)}(t-t_1, t-t_2, t-t_3) = \sum_{\alpha} R_{\alpha}^{(3)}(t-t_1, t-t_2, t-t_3)$$

2DES: off-diagonal cross-peaks resolve couplings between states

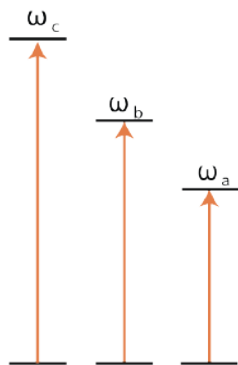


2DES: off-diagonal cross-peaks resolve couplings between states

(a)

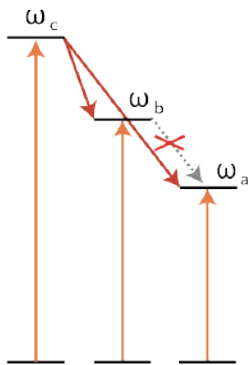
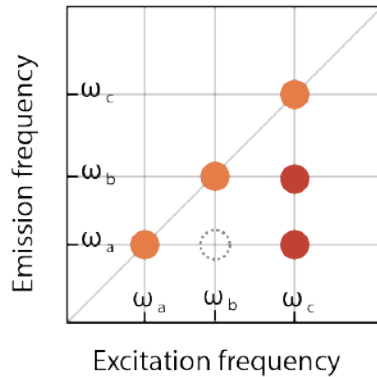


A system that produces multiple diagonal peaks but no cross-peaks can be modeled as a set of isolated non-interacting two-level systems.



2DES: off-diagonal cross-peaks resolve couplings between states

(b)

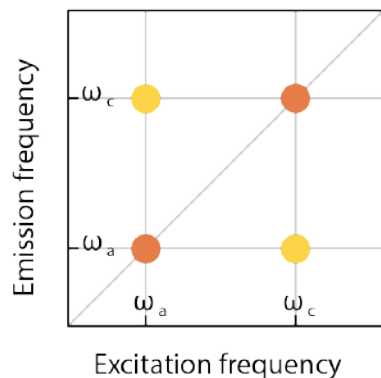


The cross-peaks at coordinates (ω_c, ω_b) and (ω_c, ω_a) appearing at $t_2 > 0$ indicate that state **c** is coupled *via* energy transfer with states **a** and **b** (Forster energy transfer, FRET).

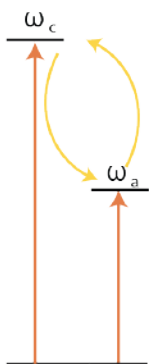
No coupling between states **a** and **b** because no cross peak appears at (ω_b, ω_a) .

2DES: off-diagonal cross-peaks resolve couplings between states

(c)

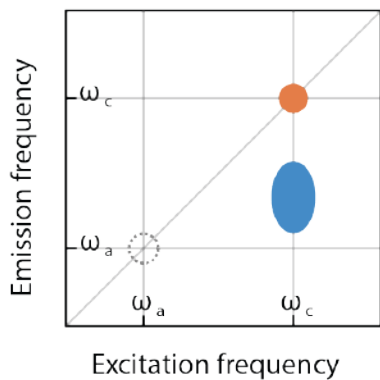


In the presence of resonance interactions between the two states, symmetric above and below diagonal cross-peaks appear already at $t_2=0$: the system can be modeled as a molecular (excitonic) dimer.

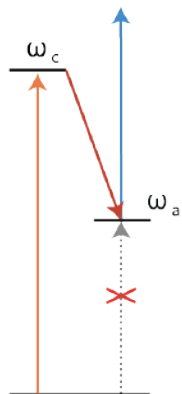


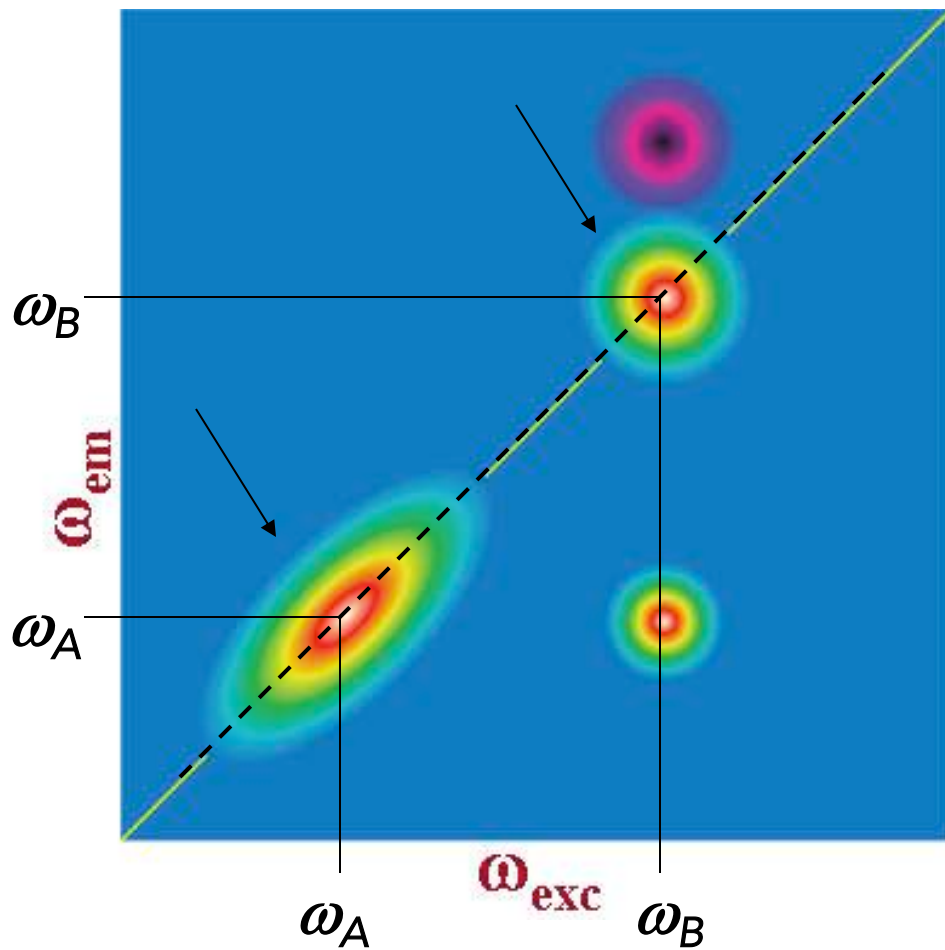
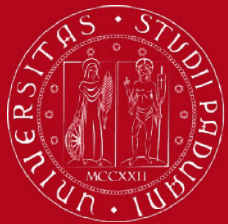
2DES: off-diagonal cross-peaks resolve couplings between states

(d)



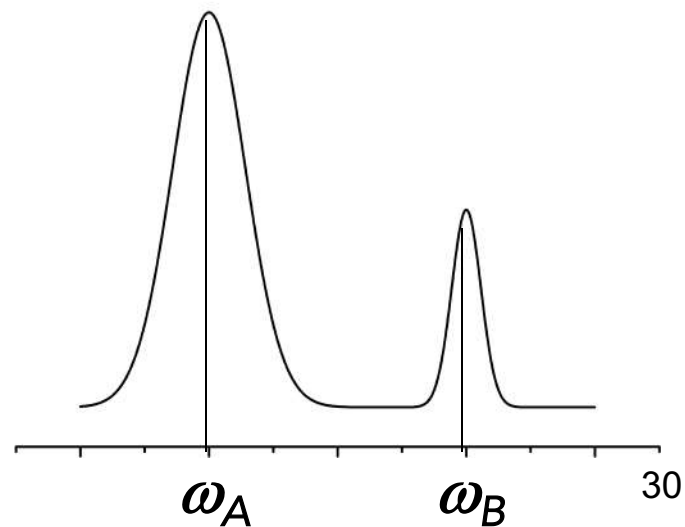
A dark state (ω_a) can be characterized by the coupling with a bright state (ω_c) in excited state absorption processes.

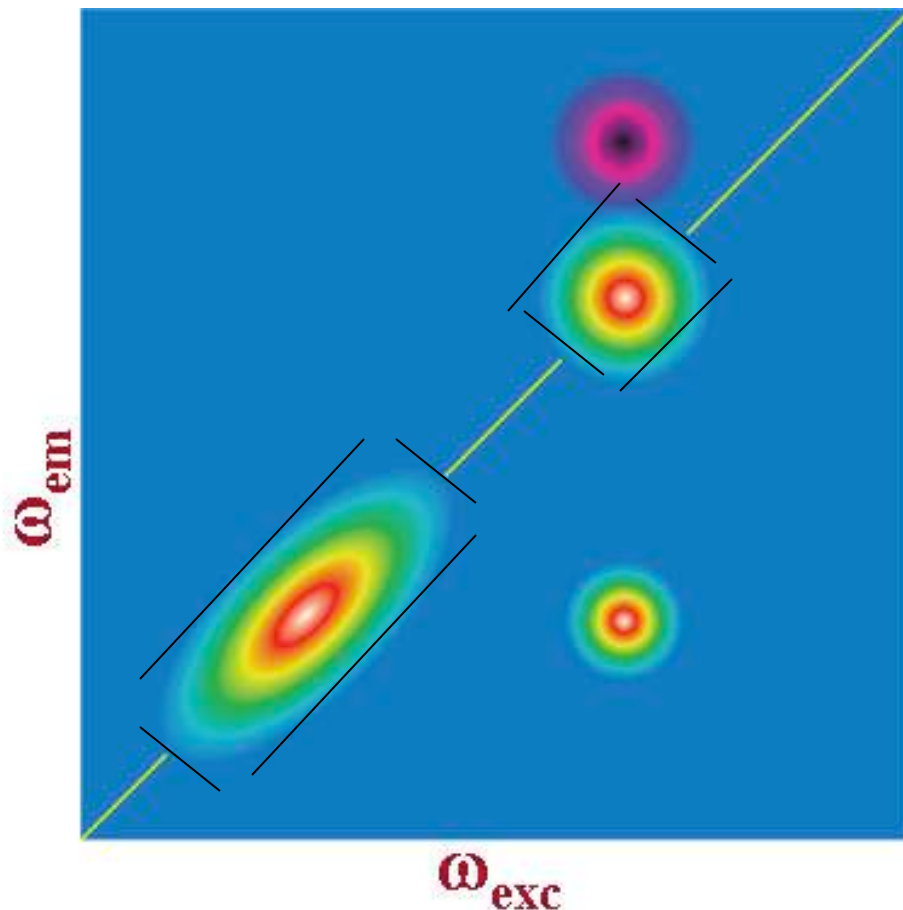




The diagonal section corresponds to linear spectrum.

diagonal peaks
↓
absorption peaks

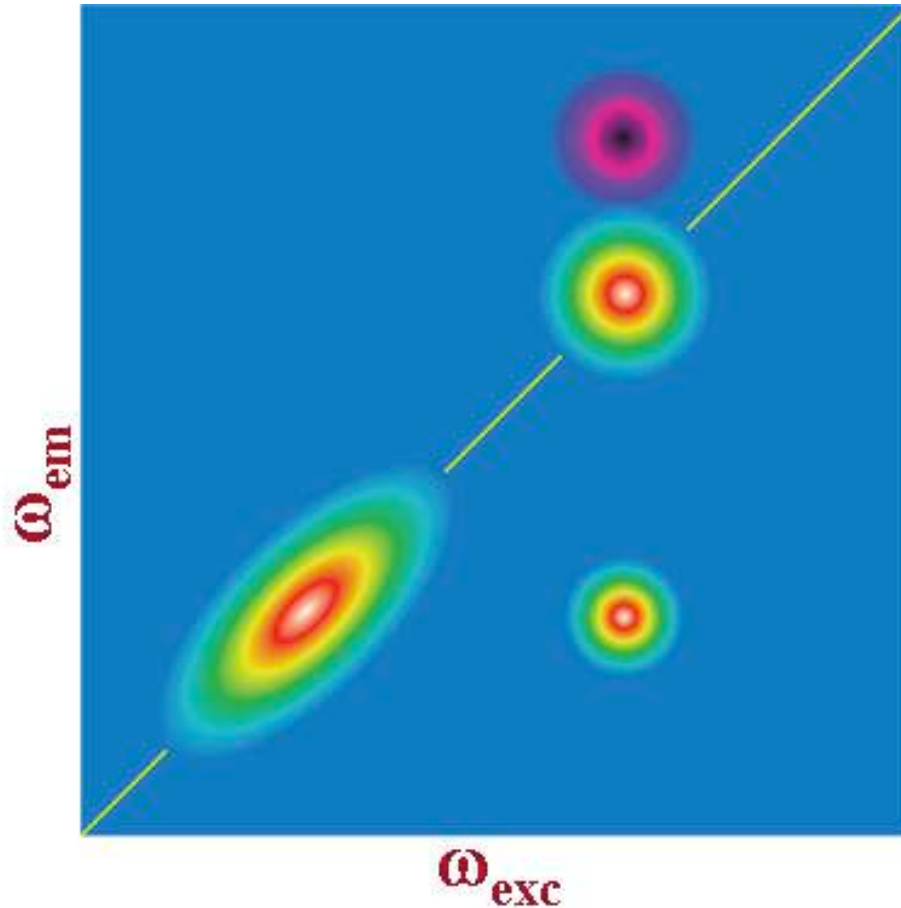




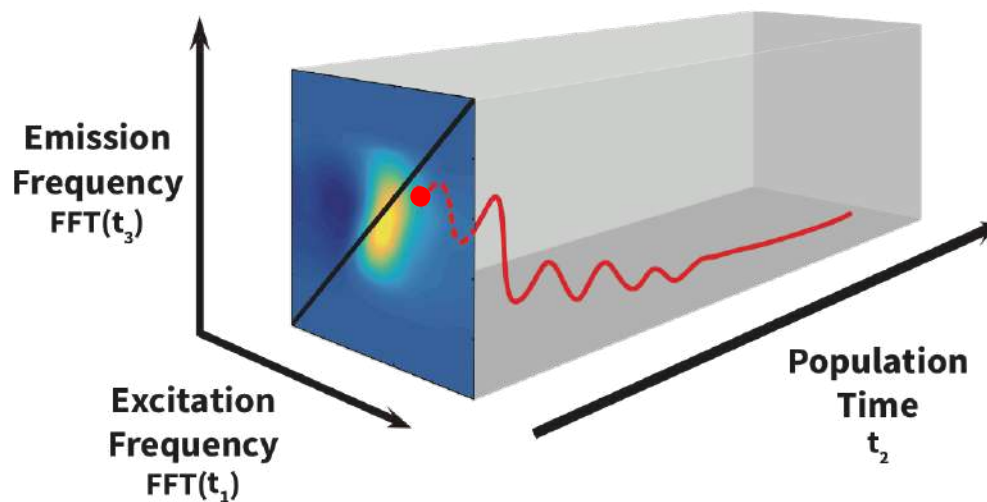
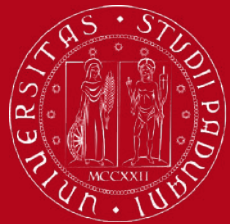
Shape of the 2D spectrum reveals distribution of the environments.

Inhomogeneous broadening: diagonal peak width

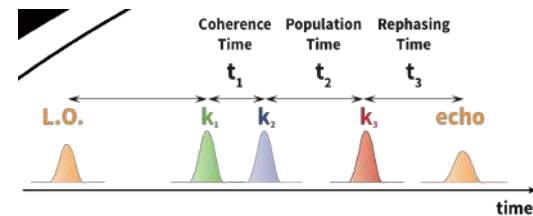
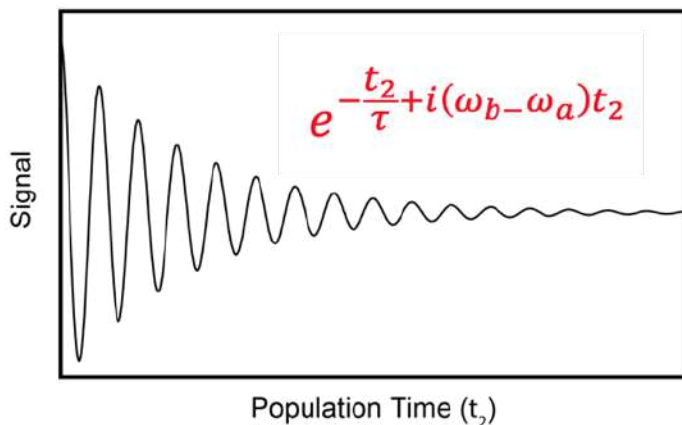
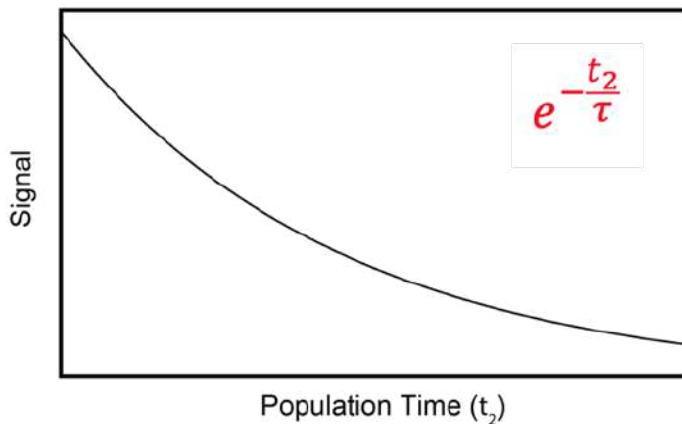
Homogeneous width: anti-diagonal peak width



If we integrate the 2D map along the ω_{exc} dimension we obtain a response equivalent to pump-probe

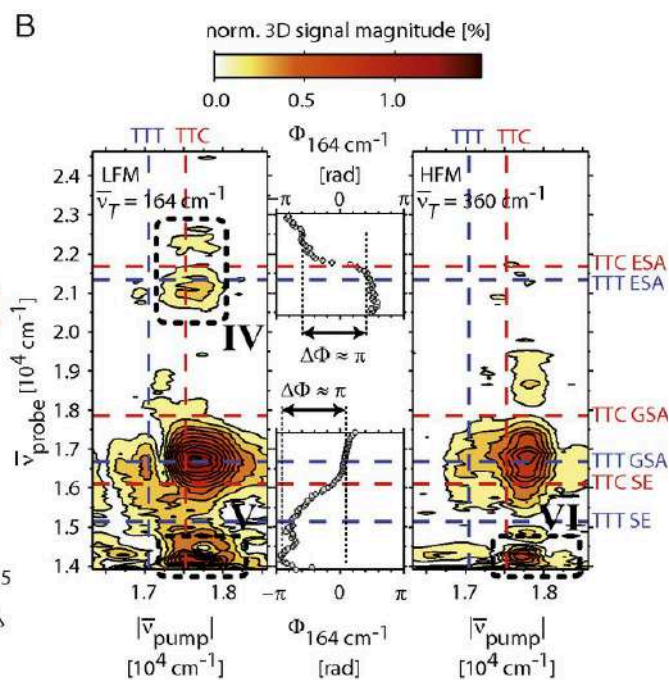
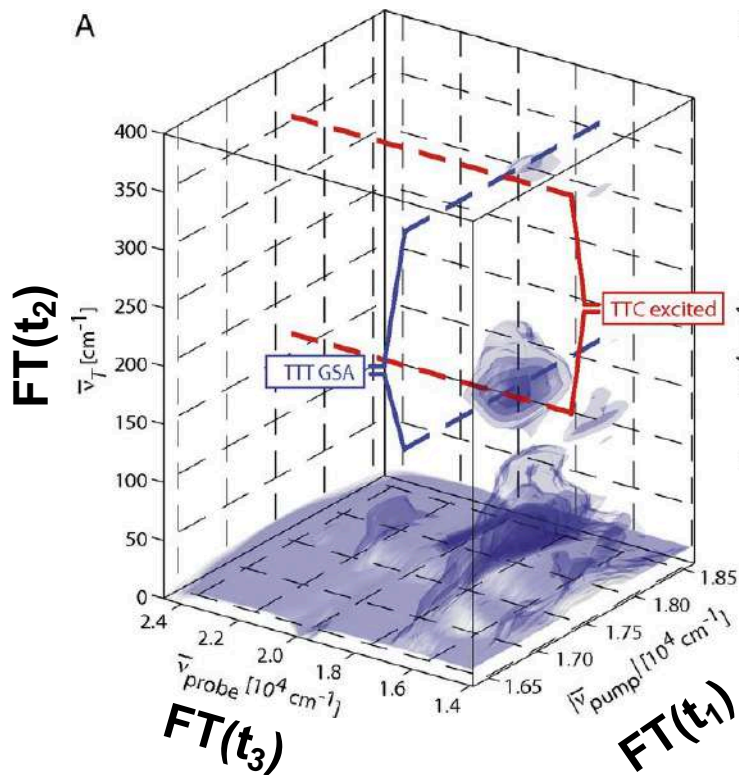


coherence and population dynamics



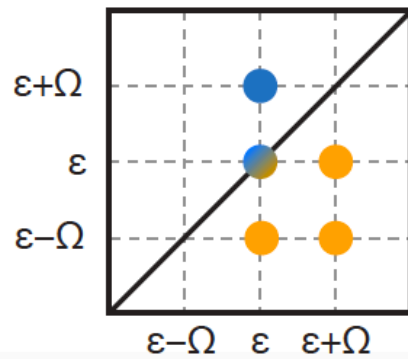
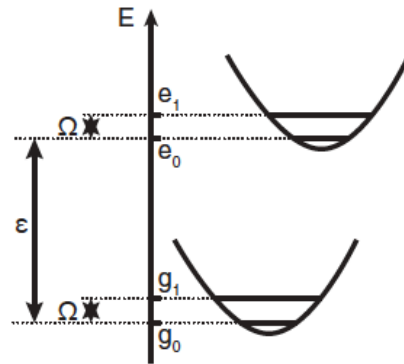
$$\begin{aligned} \psi(t) &= c_a |\psi_a(t)\rangle + c_b |\psi_b(t)\rangle \\ &= c_a |\varphi_a\rangle e^{-i\omega_a t} + c_b |\varphi_b\rangle e^{-i\omega_b t} \end{aligned}$$

$$P(t) = |\psi(t)|^2 \propto \cos(\omega_a - \omega_b)t$$

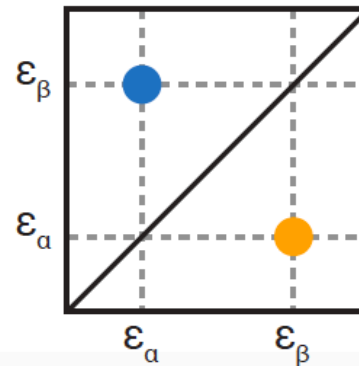
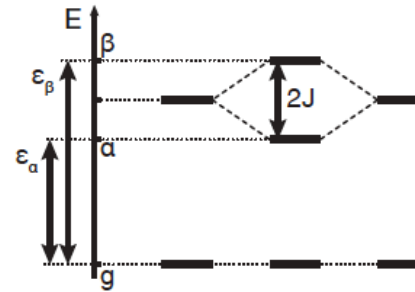


Fourier maps

VIBRATIONS



EXCITONS



applications: photosynthetic antennas

a fascinating (and still debated!) hypothesis: 'wavelike' EET

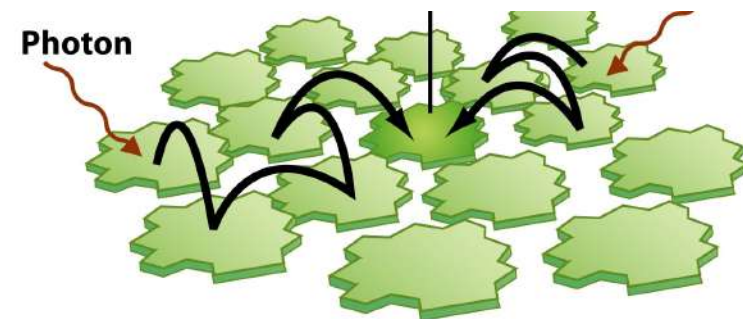
nature

Vol 446 | 12 April 2007 | doi:10.1038/nature05678

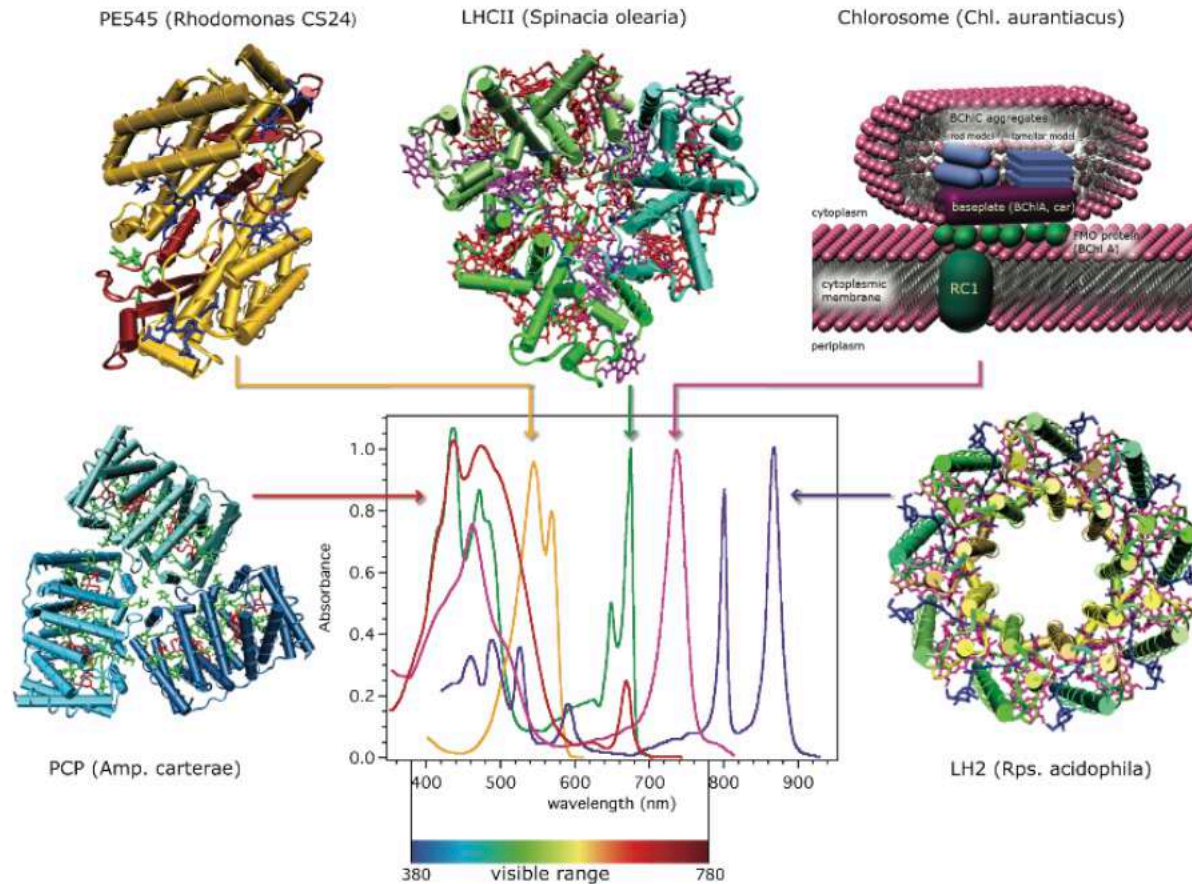
LETTERS

Evidence for wavelike energy transfer through quantum coherence in photosynthetic systems

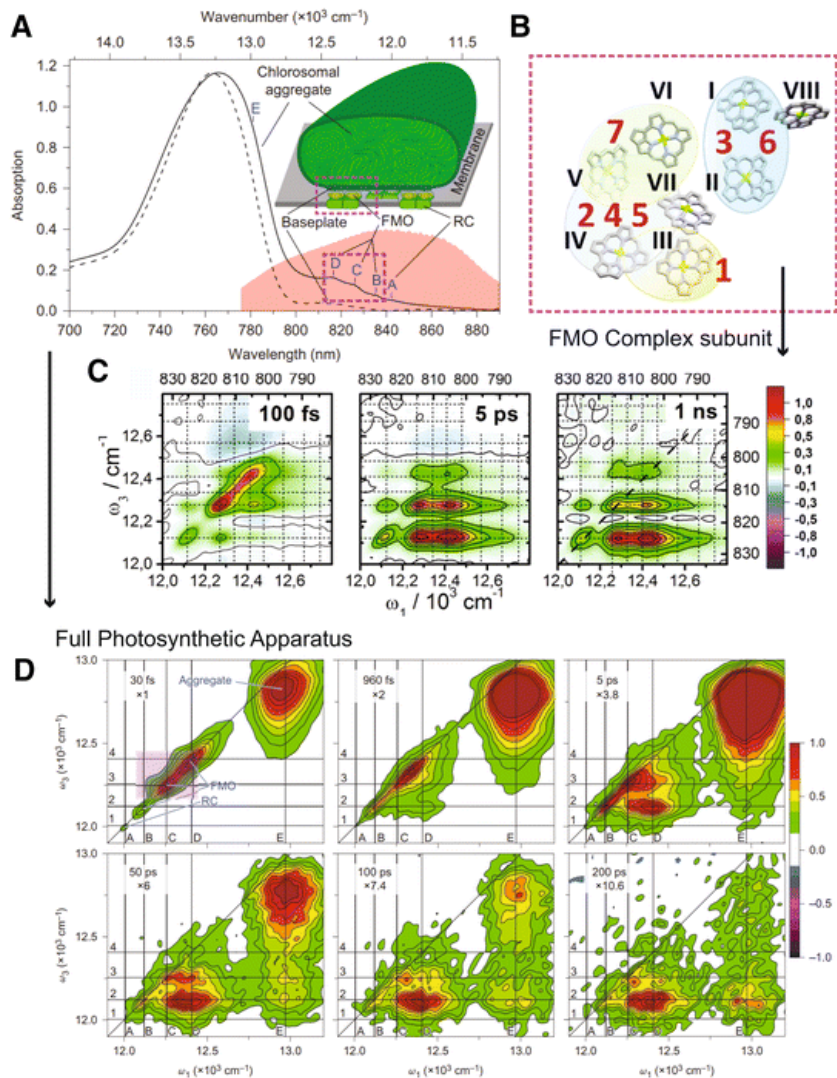
Gregory S. Engel^{1,2}, Tessa R. Calhoun^{1,2}, Elizabeth L. Read^{1,2}, Tae-Kyu Ahn^{1,2}, Tomáš Mančal^{1,2}†, Yuan-Chung Cheng^{1,2}, Robert E. Blankenship^{3,4} & Graham R. Fleming^{1,2}



overview of biological antennas

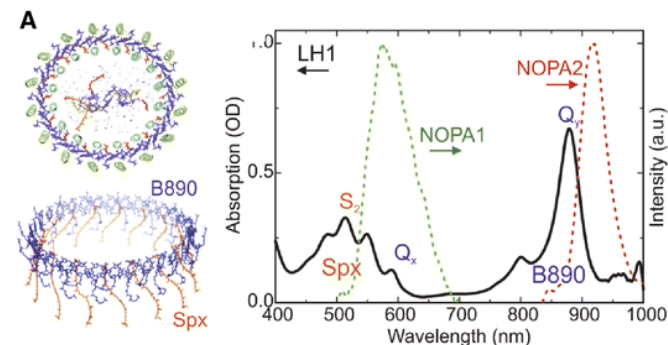


FMO (green sulfur bacteria)



2DES provided a complete picture on how the energy transfer cascade evolves from the light harvesting antenna complex to the reaction center.

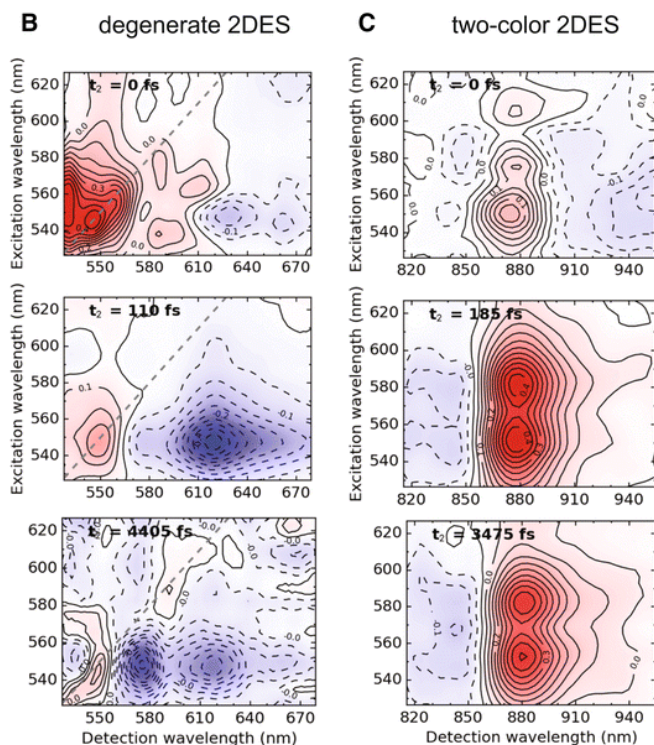
it was possible to track the step-by-step energy flow through the entire unit and observed for the first time that the FMO complex serves as energy conduit between the chlorosome and the RC.

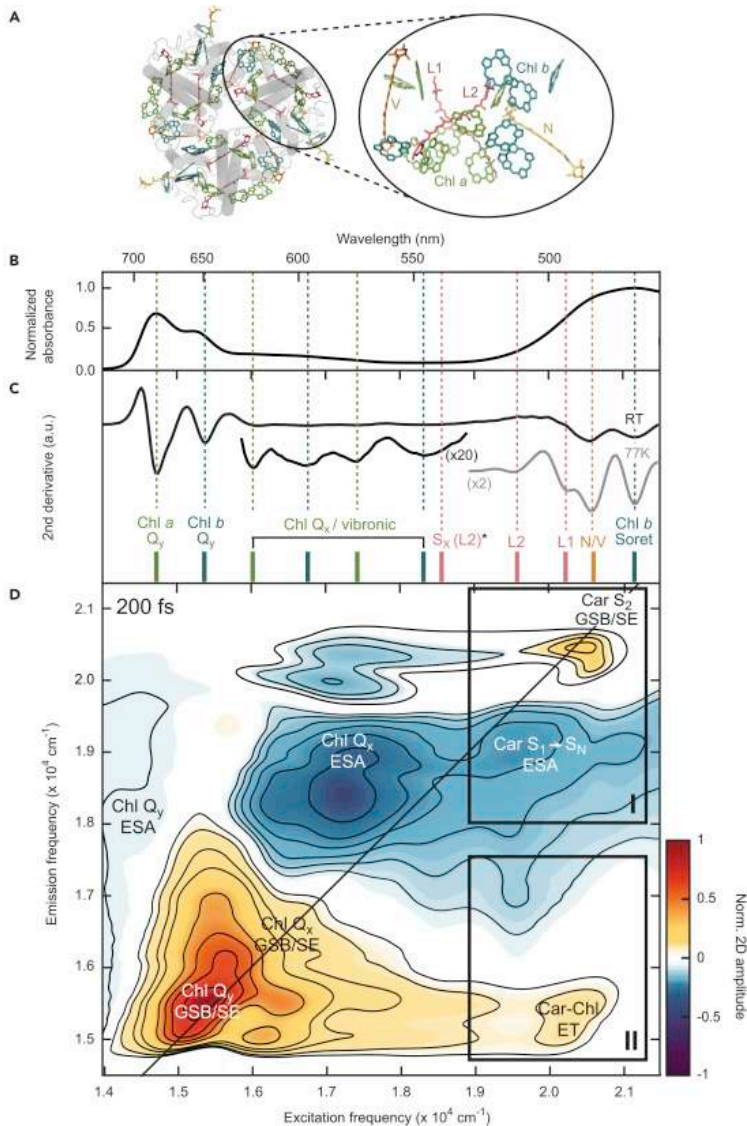


By exciting in the visible range and detecting over both visible and near-IR ranges (2-colors 2DES), it was possible to follow all the photoinduced processes:

- i) the Spx internal conversion,
- ii) the BChl $Q_x \rightarrow Q_y$ internal conversion,
- iii) the Spx \rightarrow B890 EET process

by tracking the formation of several cross-peaks in the 2DES maps.

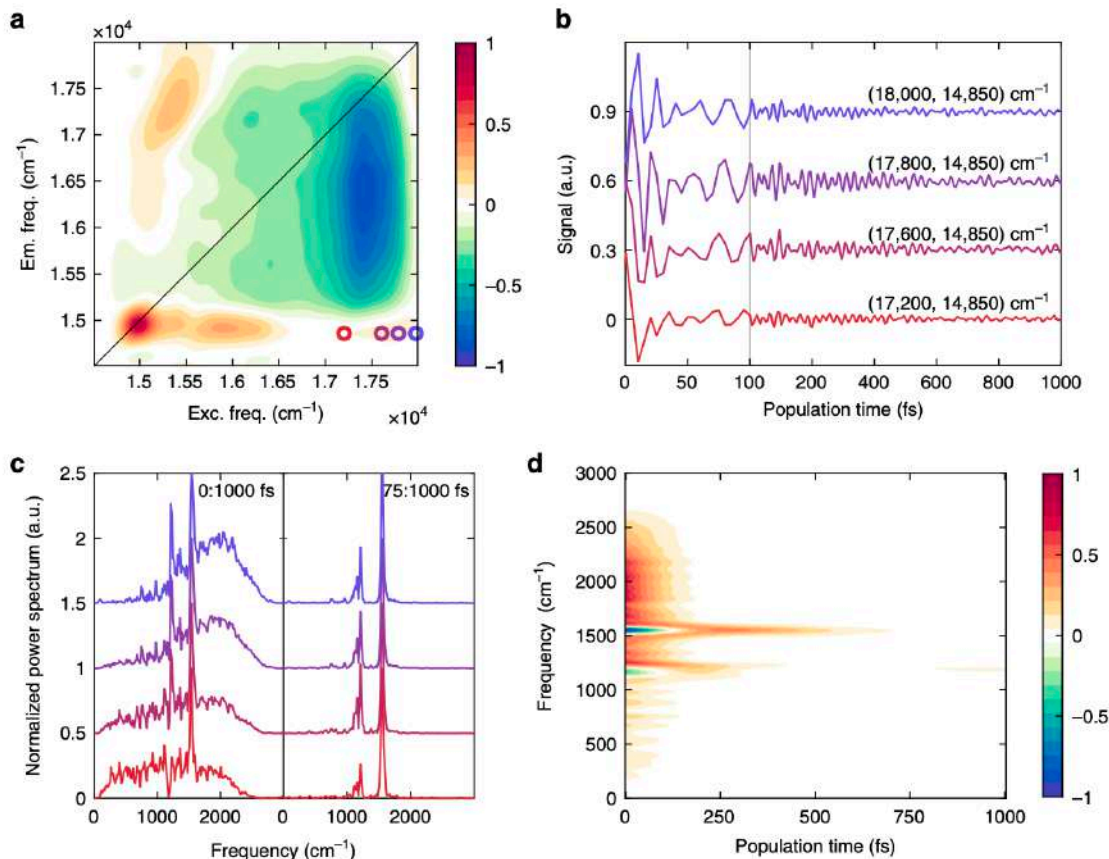
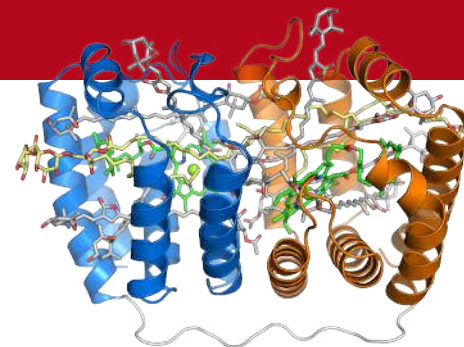




lutein 2 provides a nexus for light harvesting, collecting energy from higher-lying states and funneling it downhill, partially via a debated dark state observed exclusively on lutein 2.

These results show that the protein pocket can tune Car electronic structure via tuning the geometry, a mechanism by which plants control the photophysics of solar energy capture.

PCP (brown algae)

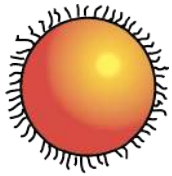


complete mapping of the multiple pathways mechanism of energy flow in PCP, and the relative time constants.

the evolution of the coherence effectively moves the population on the Q_y state: the presence of coherence appears functional to the energy distribution in PCP!

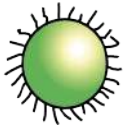
This is important information in current efforts to evaluate possible opportunities to harness coherence to realize, control, and/or drive energy transduction.

applications: quantum dots

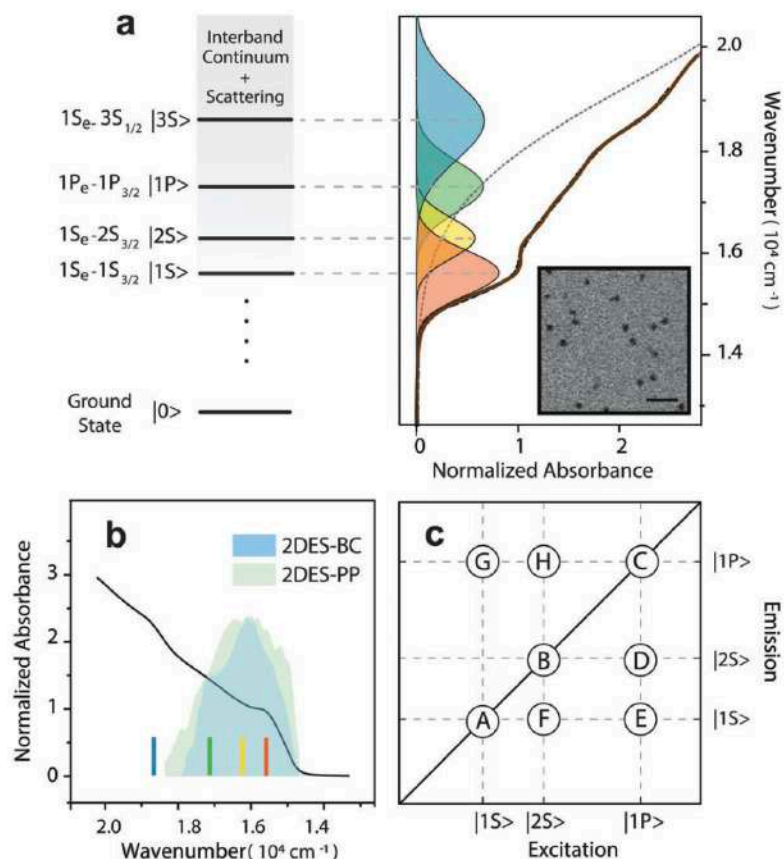


CdSe quantum dots (QDs)

Versatile systems:
photophysical properties tuned modulating
size and ligands/solvent



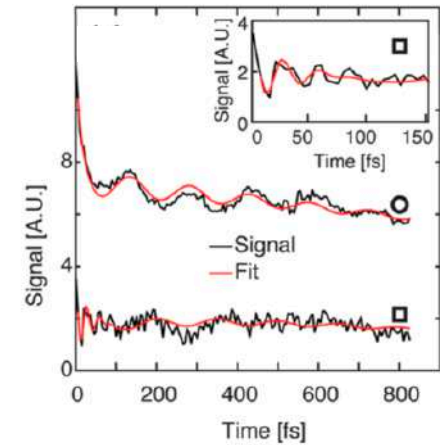
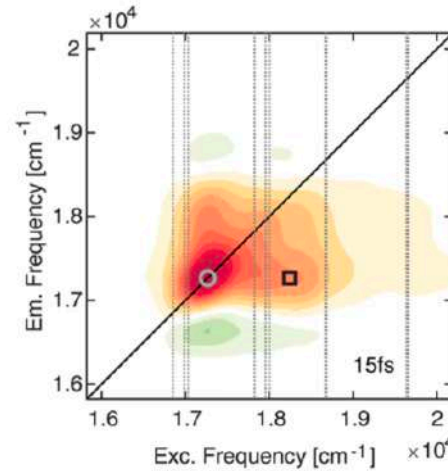
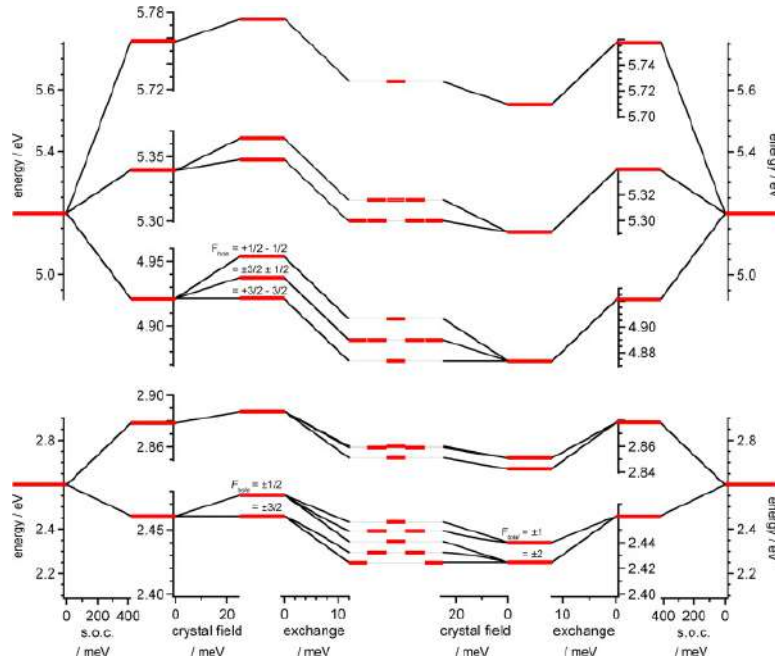
Desired properties:
Stable, processable, dense manifold of
states



core/shell CdSe/ZnS QDs

« 2D electronic spectroscopy techniques can successfully and efficiently dispel the intertwined dynamics of fast and ultrafast recombination processes in nanomaterials.

Hence, we propose this analysis scheme to be used in future research on novel quantum confined systems »



J. Phys. Chem. C 2019, 123, 31286–31293

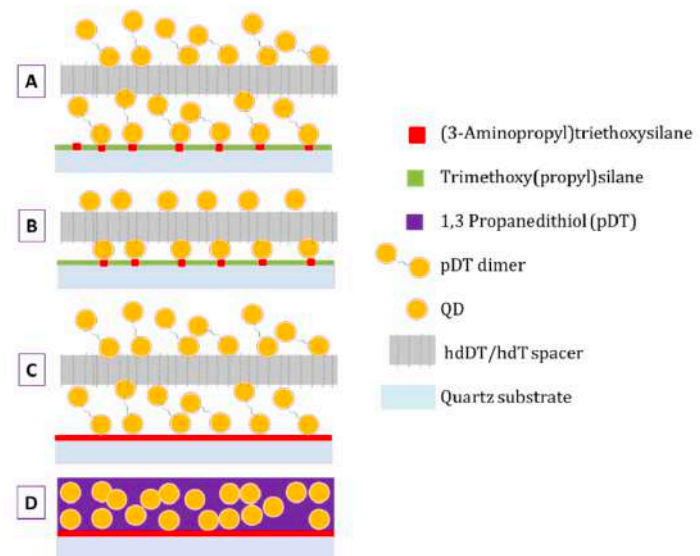
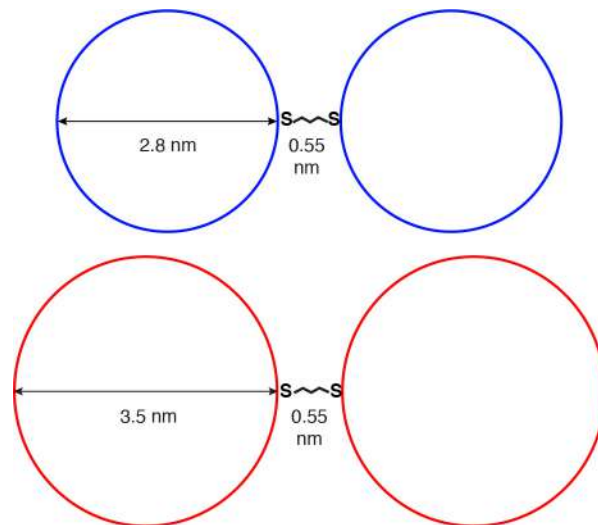
CY Wong et al., J. Luminescence, 131 366-374, 2011

2DES is sensitive to FINE STRUCTURE of QDs through the detection of the evolution of superposition of electronic states

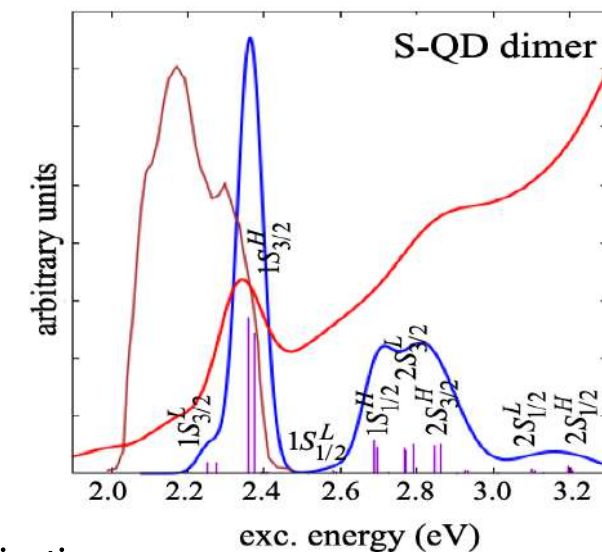
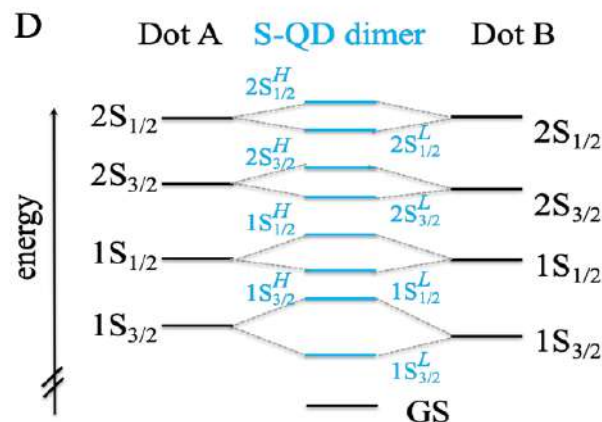
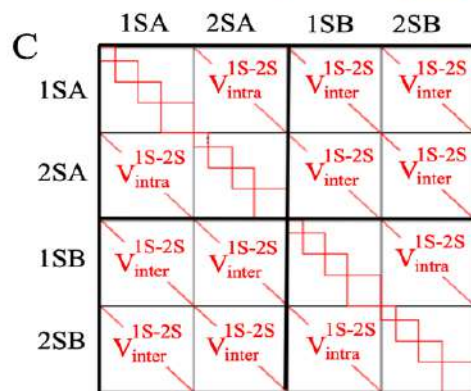
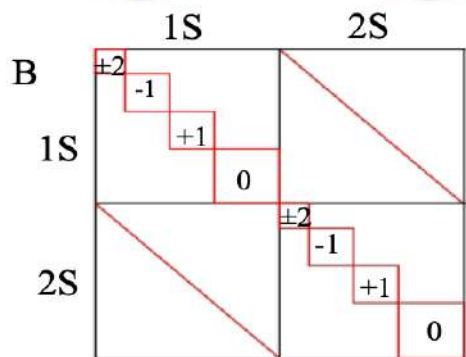
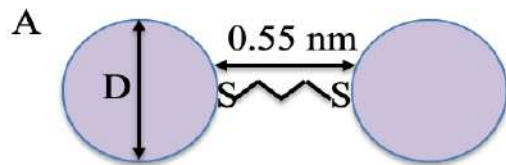
Signatures of intra-dot coherences evolution

Increasing complexity: QDs dimers

dimers of QDs in solution and solid state. The coupling between dots is modulated through the length of the coupling ligand (di-thiol)



Interest: interacting QDs with delocalized wavefunctions and engineered coherences for applications in quantum technologies

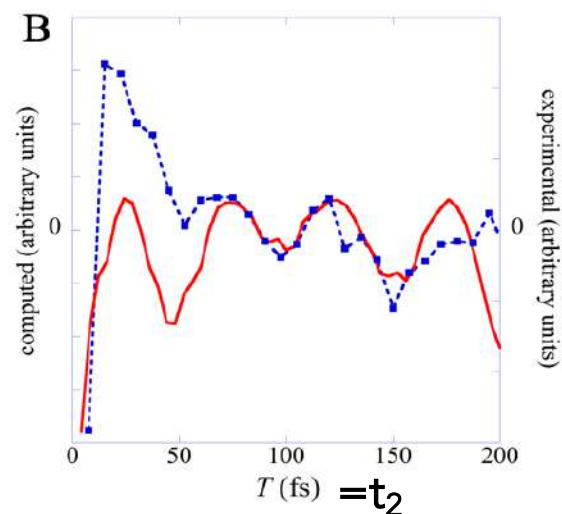
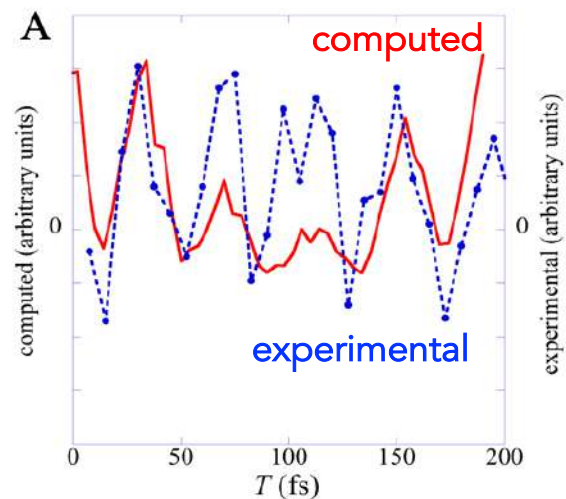
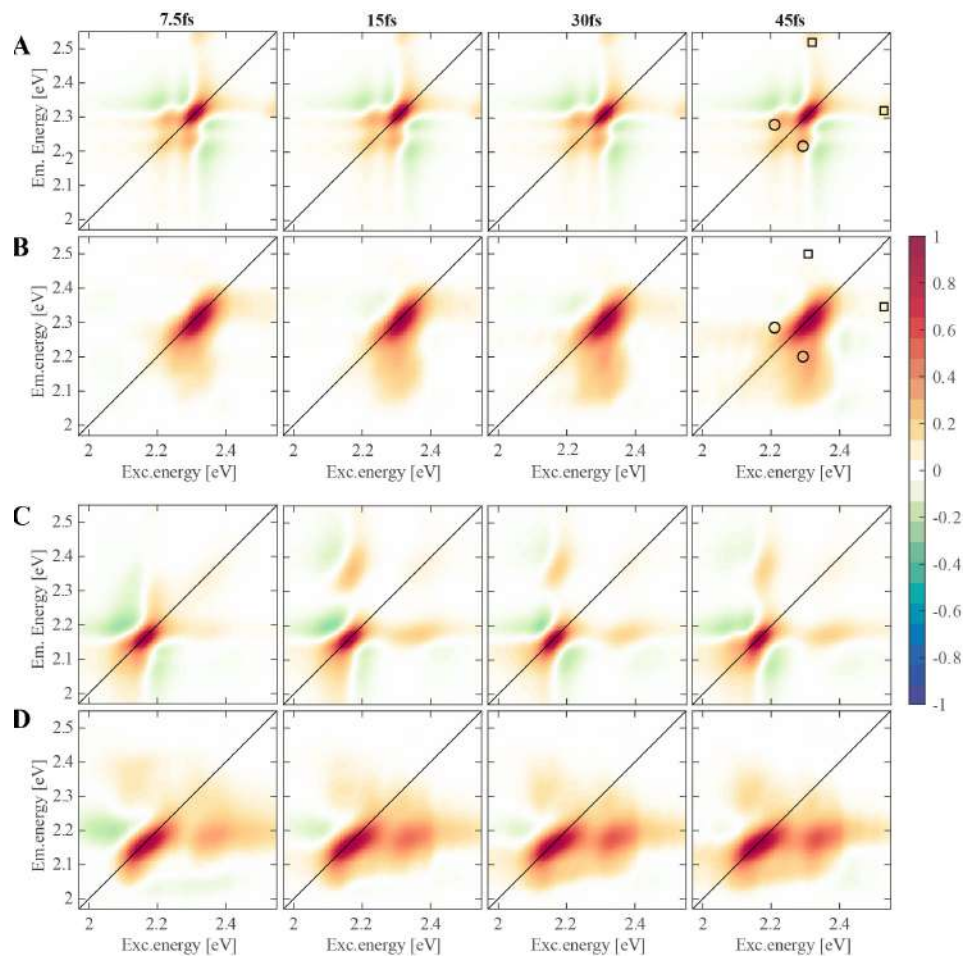


Simulations suggested important guidelines for the design of materials with wanted coherent properties:

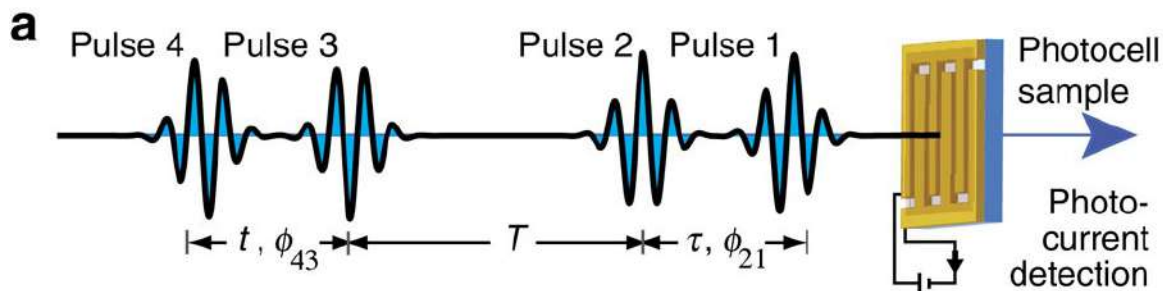
- Short distance
- Small size
- Limited size distribution (5% optimal)



QDs dimers: inter-dot coherences



applications: working devices

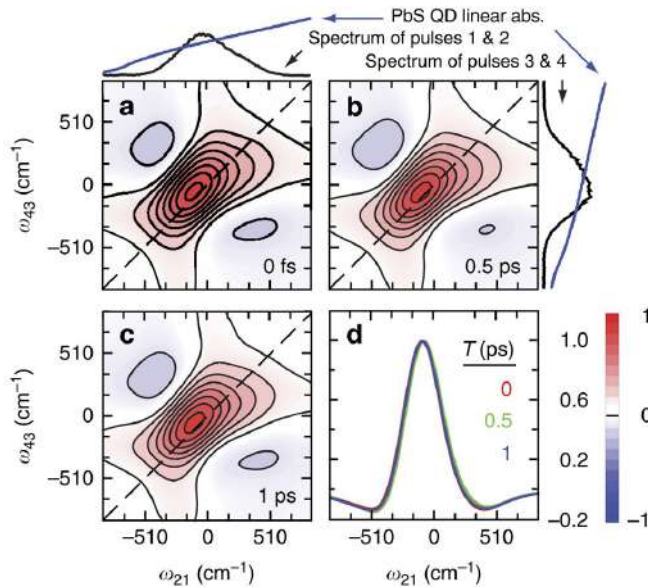


collinear setup (exciting pulses propagate along the same direction)

a fourth pulse is added to the pulse sequence to drive the system into an excited or ground state population.

phase modulation or phase cycling schemes: the phases of the excitation pulses are independently varied by controlled amounts; the excited state population is also modulated, and then it can be read out by some other means, for example, photocurrent or photoluminescence.

Possibility for mass spectrometry detection (and many others detection schemes!) and single molecules implementations



sub-picosecond evolution of two-dimensional spectra consistent with multiple exciton generation

selective spectroscopic information about the coherences and populations that contribute to the final observable, which can be important to understand how and which electronically excited material states are most relevant to the function of an optical or optoelectronic device.

